
Diffraction contrast imaging

Lecture 12 Part 2

Review: Planar faults
Strain fields - generally
Dislocations
Coherent precipitates

Strain fields

As with planar faults, strain fields also introduce changes in the location of atoms within the crystal

In other words, any strain field introduces an $\vec{R}(\vec{r}_n')$, where:

$$\vec{r}_n' = \vec{r}_n + \vec{R}_n$$

Location of defective unit cell \longrightarrow \vec{r}_n'

Regular lattice positions \longleftarrow \vec{r}_n

Displacement function \longleftarrow \vec{R}_n

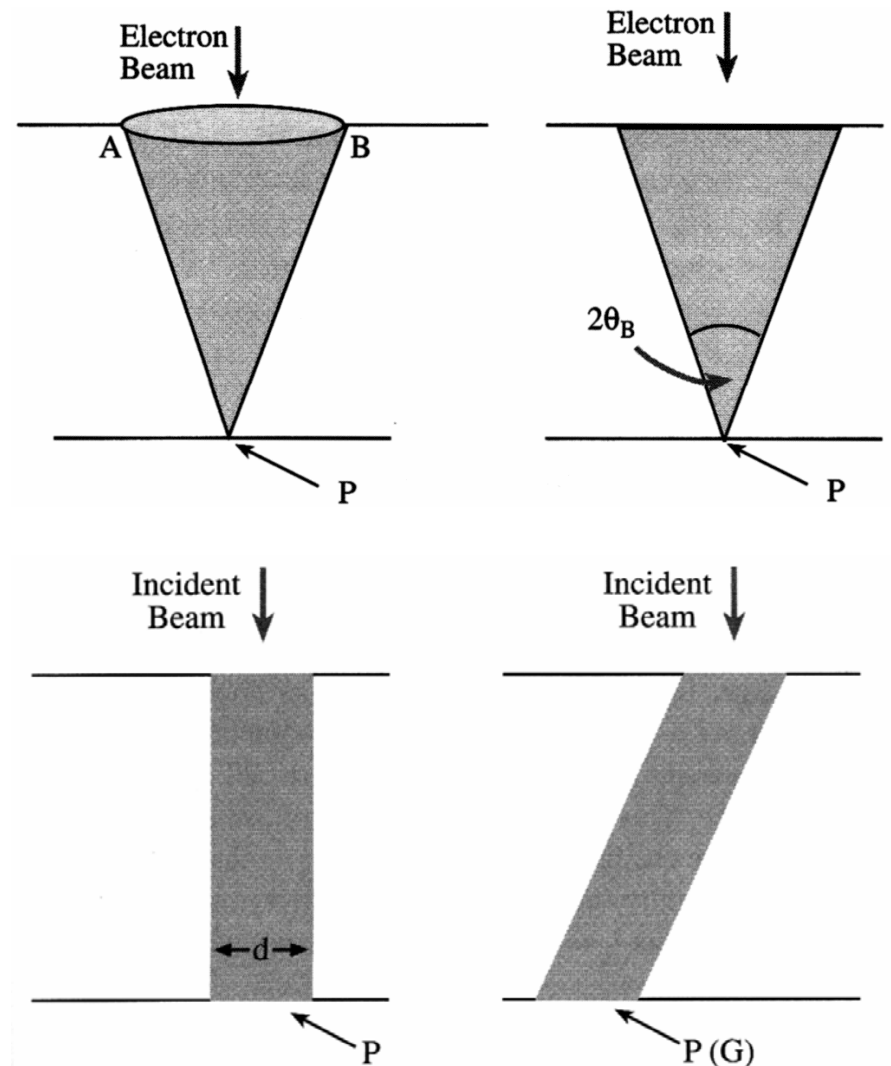
With planar faults, the shift between one lattice and the next is single valued

What happens if the strain field is continuous?

Calculating dislocation contrast

We use the “column approximation”

This is where we said we’d ignore variations in dz with changes in z



Modification of H-W Eqns

Possible to re-write the H-W Eqns in a different form, which incorporates a continuous $\vec{R}(\vec{r}_n')$

Use a different substitution of variables than in previous derivation (planar case)

Yields:

$$\frac{d\phi_o}{dz} = \frac{\pi i}{\xi_o} \phi_g$$

and

$$\frac{d\phi_g}{dz} = \frac{\pi i}{\xi_g} \phi_o + \left[2\pi i \left(\underbrace{sz + \mathbf{g} \cdot \frac{d\mathbf{R}}{dz}}_{\mathbf{s}_R} \right) \right] \phi_g = \frac{\pi i}{\xi_g} \phi_o + 2\pi i \mathbf{s}_R \phi_g$$

$$\mathbf{s}_R = \mathbf{s}z + \mathbf{g} \cdot \frac{d\mathbf{R}}{dz}$$

Calculating dislocation contrast

So, divide the sample into narrow columns

Calculate the amplitude of ϕ_o and ϕ_g for each column

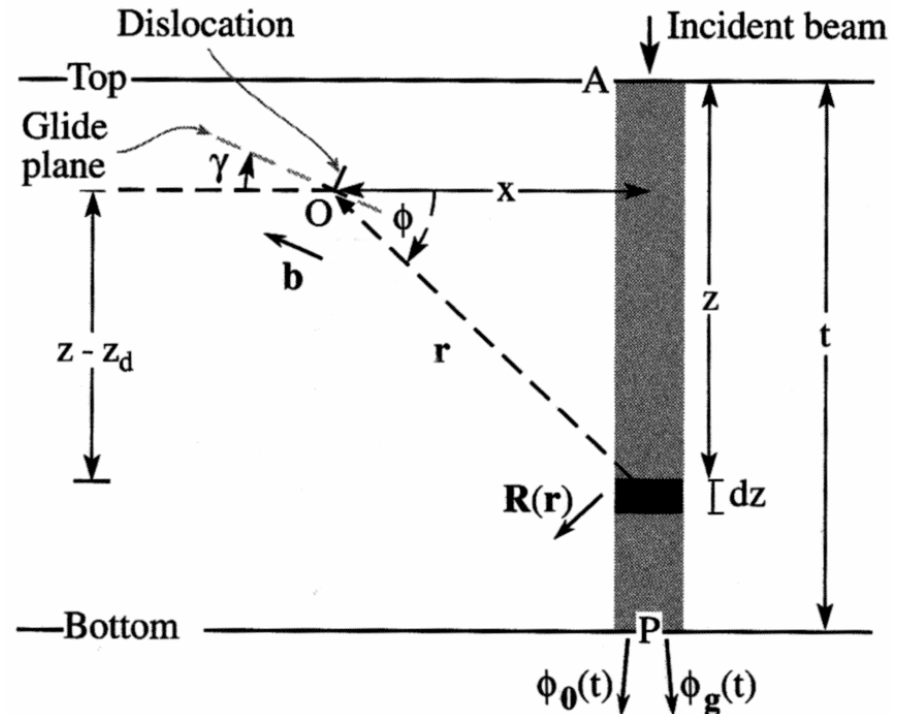
What is R?

- Need to go to elasticity theory

- Find:

$$\vec{R} = \frac{1}{2\pi} \left\{ \frac{r}{b\phi} + \frac{1}{4(1-\nu)} \left[\frac{r}{b_e} + \mathbf{b} \times \hat{u} (2(1-2\nu)\ln r + \cos 2\phi) \right] \right\}$$

- Or if doing computationally, use anisotropic elasticity theory, or simulation output



Modification of H-W Eqns

Possible to re-write the H-W Eqns in a different form, which incorporates a continuous $\vec{R}(\vec{r}_n')$

Use a different substitution of variables than in previous derivation (planar case)

Yields:

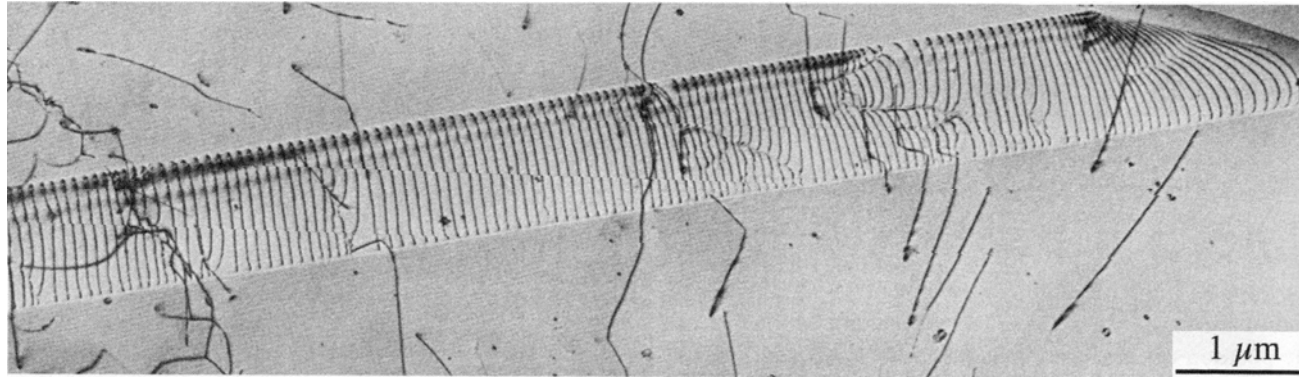
$$\frac{d\phi_o}{dz} = \frac{\pi i}{\xi_o} \phi_g$$

and

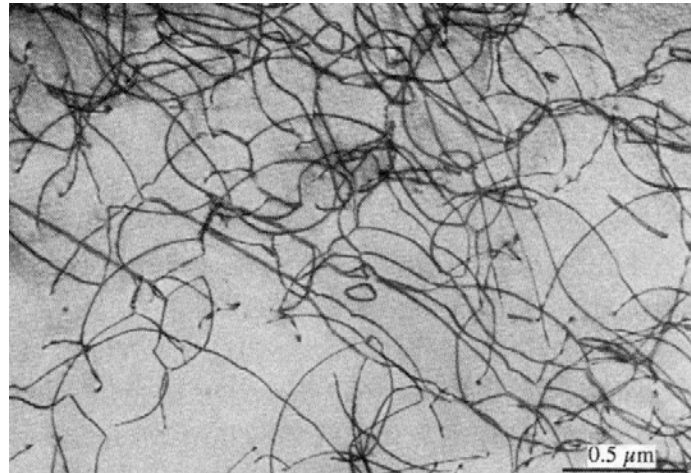
$$\frac{d\phi_g}{dz} = \frac{\pi i}{\xi_g} \phi_o + \left[2\pi i \left(\underbrace{sz + \mathbf{g} \cdot \frac{d\mathbf{R}}{dz}}_{\mathbf{s}_R} \right) \right] \phi_g = \frac{\pi i}{\xi_g} \phi_o + 2\pi i \mathbf{s}_R \phi_g$$

$$\mathbf{s}_R = \mathbf{s}z + \mathbf{g} \cdot \frac{d\mathbf{R}}{dz}$$

Dislocations interactions & tangles



HVEM Image of slip along an inclined plane



A complex dislocation tangle

Cold rolled alloy



Calculating dislocation contrast

So, divide the sample into narrow columns

Calculate the amplitude of ϕ_o and ϕ_g for each column

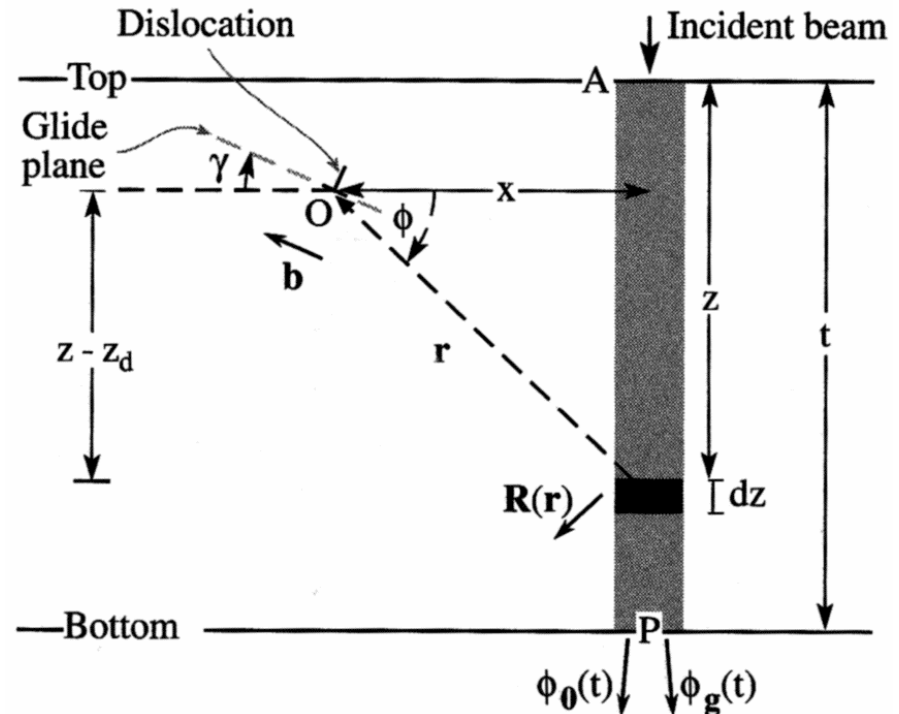
What is R ?

- Need to go to elasticity theory

- Find:

$$\vec{R} = \frac{1}{2\pi} \left\{ \frac{r}{b\phi} + \frac{1}{4(1-\nu)} \left[\frac{r}{b_e} + \mathbf{b} \times \hat{u} (2(1-2\nu)\ln r + \cos 2\phi) \right] \right\}$$

- Or if doing computationally, use anisotropic elasticity theory, or simulation output



Dislocation contrast

Consider a pure screw dislocation:

$$\vec{b}_e = 0 ; \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$$

$$\vec{R} = \dot{\mathbf{b}} \frac{\phi}{2\pi} = \frac{\dot{\mathbf{b}}}{2\pi} \tan\left(\frac{z - z_d}{x}\right)$$

So: $\vec{R} \propto \dot{\mathbf{b}}$

Thus: $\vec{g} \cdot \vec{R} \propto \vec{g} \cdot \dot{\mathbf{b}}$

“g dot b” contrast

Table 25.1. Different Burgers Vectors and Different Reflections Give Different $\mathbf{g} \cdot \mathbf{b} = n$ Values^a

$\mathbf{g} \backslash \mathbf{b}$	$\frac{1}{6} [11\bar{2}]$	$\frac{1}{6} [1\bar{2}1]$	$\frac{1}{6} [\bar{2}11]$	$\frac{1}{3} [111]$
$\pm(1\bar{1}1)$	$\pm 1/3$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$
$\pm(\bar{1}\bar{1}1)$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$	$\pm 1/3$
$\pm(0\bar{2}2)$	± 1	± 1	0	0
$\pm(200)$	$\pm 1/3$	$\pm 1/3$	$\pm 2/3$	$\pm 2/3$
$\pm(3\bar{1}1)$	0	± 1	± 1	± 1
$\pm(\bar{3}\bar{1}1)$	± 1	0	± 1	± 1

^aThe dislocations all lie on a (111) plane in an fcc material; the beam direction is [011].

Modification of H-W Eqns

Possible to re-write the H-W Eqns in a different form, which incorporates a continuous $\vec{R}(\vec{r}_n')$

Use a different substitution of variables than in previous derivation (planar case)

Yields:

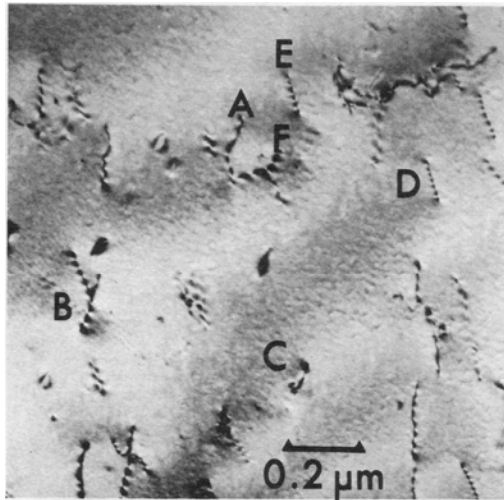
$$\frac{d\phi_o}{dz} = \frac{\pi i}{\xi_o} \phi_g$$

and

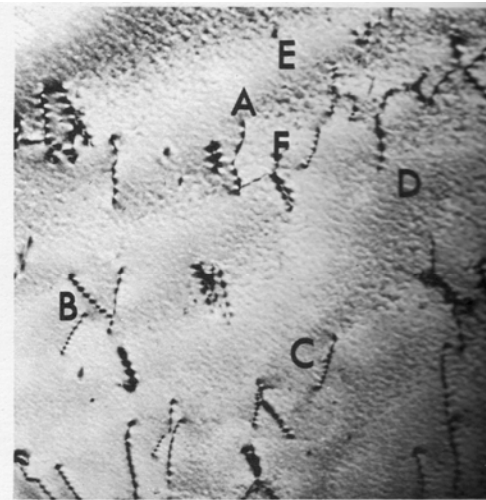
$$\frac{d\phi_g}{dz} = \frac{\pi i}{\xi_g} \phi_o + \left[2\pi i \left(\underbrace{sz + \mathbf{g} \cdot \frac{d\mathbf{R}}{dz}}_{\mathbf{s}_R} \right) \right] \phi_g = \frac{\pi i}{\xi_g} \phi_o + 2\pi i \mathbf{s}_R \phi_g$$

$$\mathbf{s}_R = \mathbf{s}z + \mathbf{g} \cdot \frac{d\mathbf{R}}{dz}$$

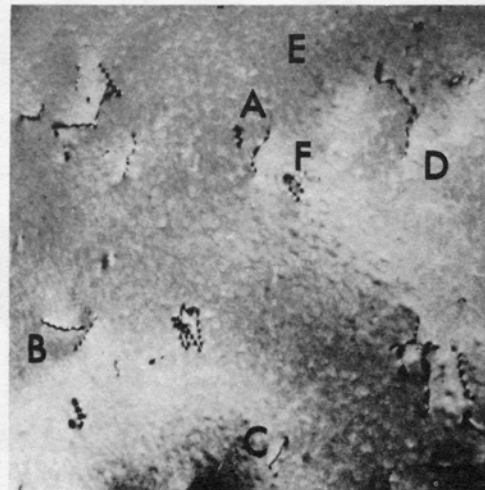
Dislocation contrast



(a)



(b)



(c)

Dislocation contrast

Consider a pure screw dislocation:

$$\vec{b}_e = 0 ; \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$$

$$\vec{R} = \dot{\mathbf{b}} \frac{\phi}{2\pi} = \frac{\dot{\mathbf{b}}}{2\pi} \tan\left(\frac{z - z_d}{x}\right)$$

So: $\vec{R} \propto \dot{\mathbf{b}}$

Thus: $\vec{g} \cdot \vec{R} \propto \vec{g} \cdot \dot{\mathbf{b}}$

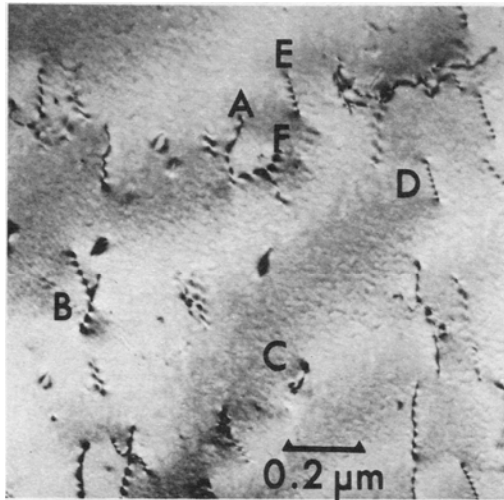
“g dot b” contrast

Table 25.1. Different Burgers Vectors and Different Reflections Give Different $\mathbf{g} \cdot \mathbf{b} = n$ Values^a

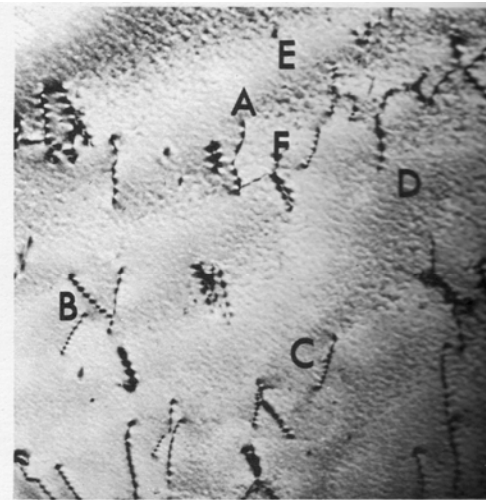
$\mathbf{g} \backslash \mathbf{b}$	$\frac{1}{6} [11\bar{2}]$	$\frac{1}{6} [1\bar{2}1]$	$\frac{1}{6} [\bar{2}11]$	$\frac{1}{3} [111]$
$\pm(1\bar{1}1)$	$\pm 1/3$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$
$\pm(\bar{1}\bar{1}1)$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$	$\pm 1/3$
$\pm(0\bar{2}2)$	± 1	± 1	0	0
$\pm(200)$	$\pm 1/3$	$\pm 1/3$	$\pm 2/3$	$\pm 2/3$
$\pm(3\bar{1}1)$	0	± 1	± 1	± 1
$\pm(\bar{3}\bar{1}1)$	± 1	0	± 1	± 1

^aThe dislocations all lie on a (111) plane in an fcc material; the beam direction is [011].

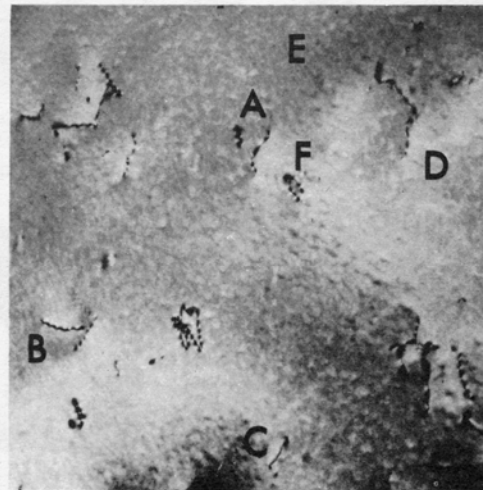
Dislocation contrast



(a)



(b)



(c)

Dislocation contrast

Now for pure edge

$$\vec{b} = b_e \hat{u} ; b_e \times \hat{u} \neq 0$$

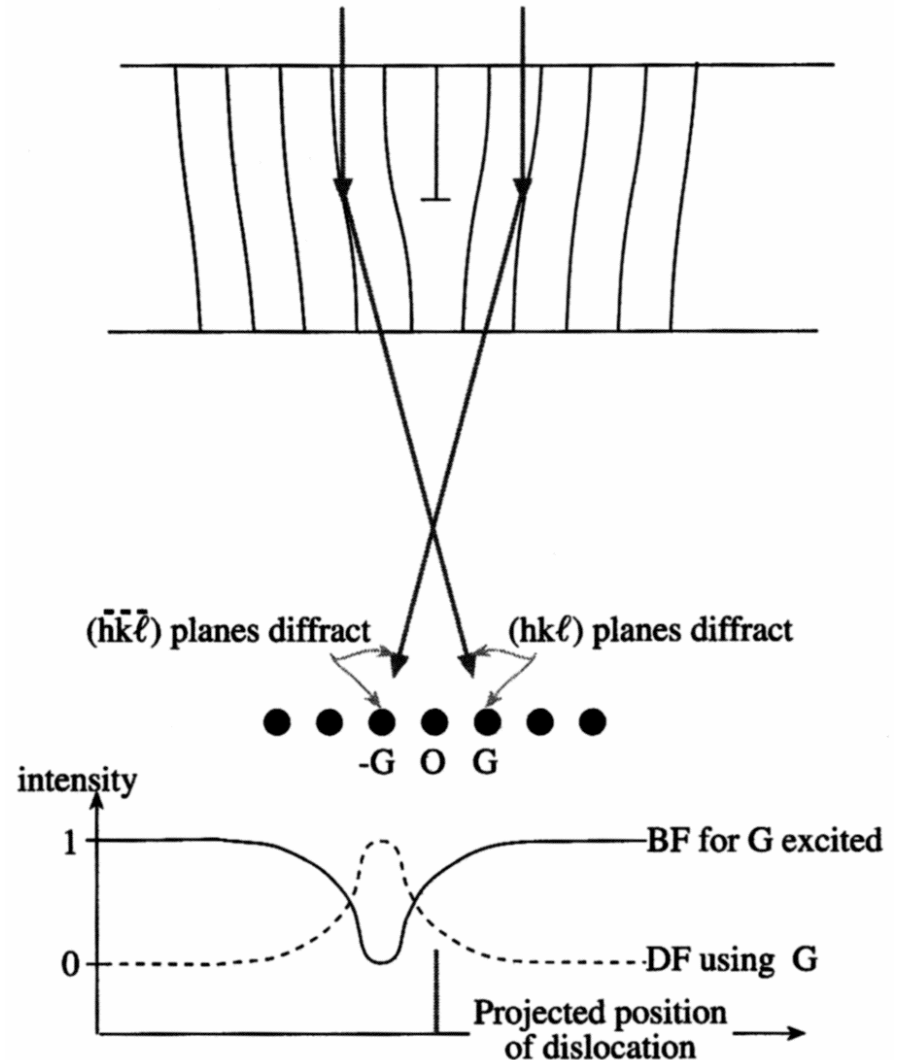
So R has both a $\vec{g} \cdot \vec{b}$ & a $\vec{g} \cdot \vec{b} \times \hat{u}$ term

More on 'g dot b' contrast

Often said that when $\vec{g} \cdot \vec{b} = 0$ the dislocation is 'invisible'

This is because the lattice distortion is on diffracting planes parallel to R

– You won't see it's effect



Dislocation contrast

More to it (unfortunately)

Firstly, what is 'invisible'?

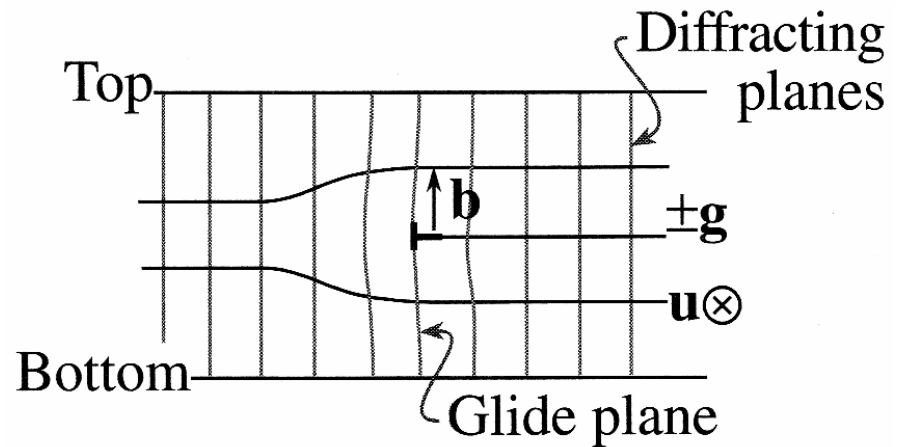
Generally if $\vec{g} \cdot \vec{b} < \frac{1}{3}$ the contrast is faint

More importantly, even if

$\vec{g} \cdot \vec{b} = 0$ can have $\vec{g} \cdot \vec{b} \times \vec{u} \neq 0$

So, really need to find conditions where both $\vec{g} \cdot \vec{b} = 0$ & $\vec{g} \cdot \vec{b} \times \vec{u} = 0$ if possible

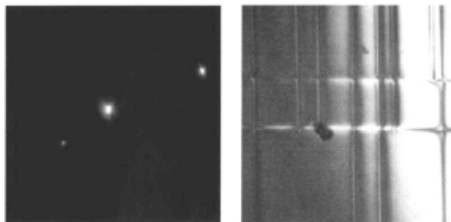
May have to settle for $\vec{g} \cdot \vec{b} = 0$ & $\vec{g} \cdot \vec{b} \times \vec{u} \leq 0.64$



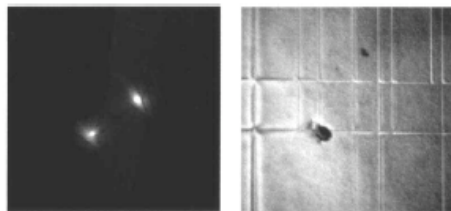
Surface effects & interfaces

311 two beam condition
Images are axial dark field

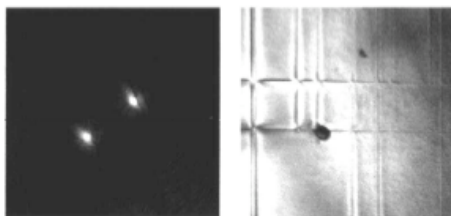
$s \gg 0$



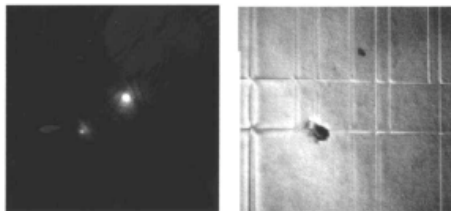
$s > 0$



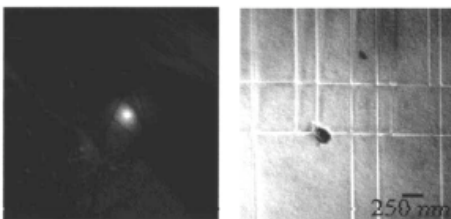
$s = 0$



$s < 0$

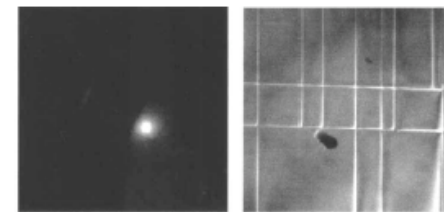


$s \ll 0$

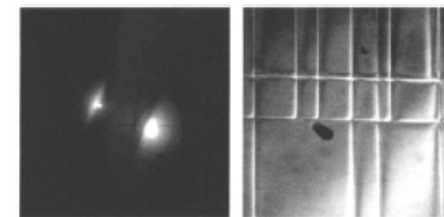


$13\bar{1}$ two beam condition
Images are axial dark field

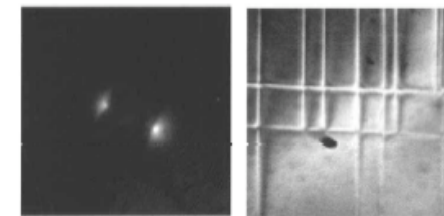
$s \gg 0$



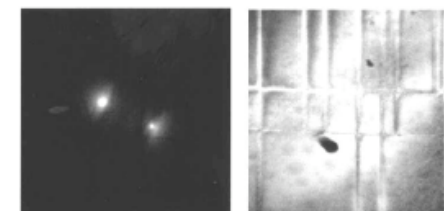
$s > 0$



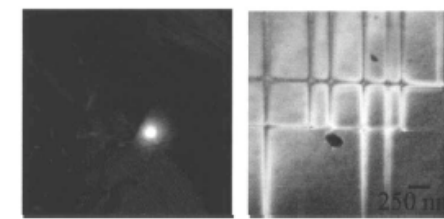
$s = 0$



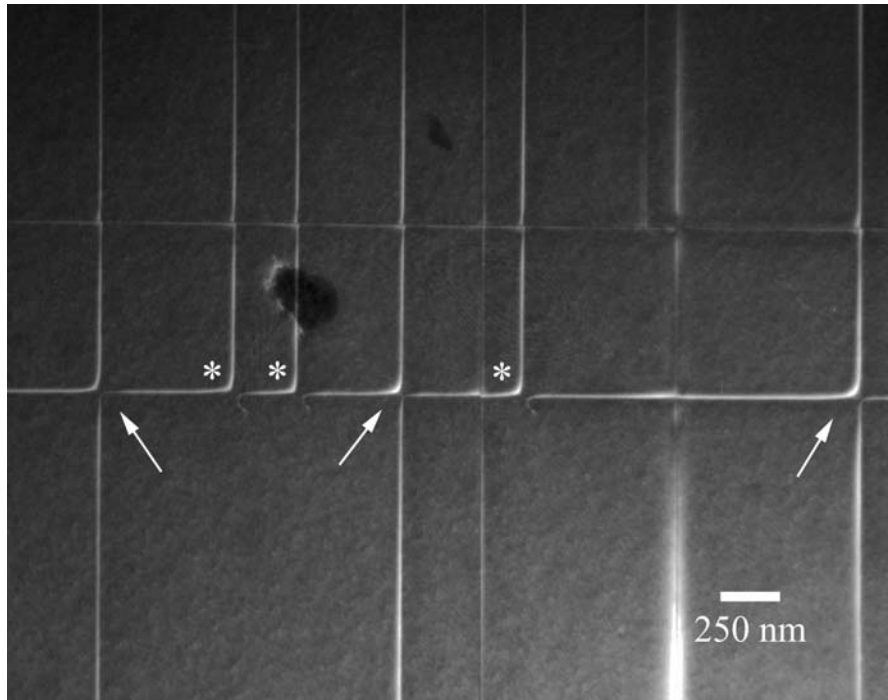
$s < 0$



$s \ll 0$

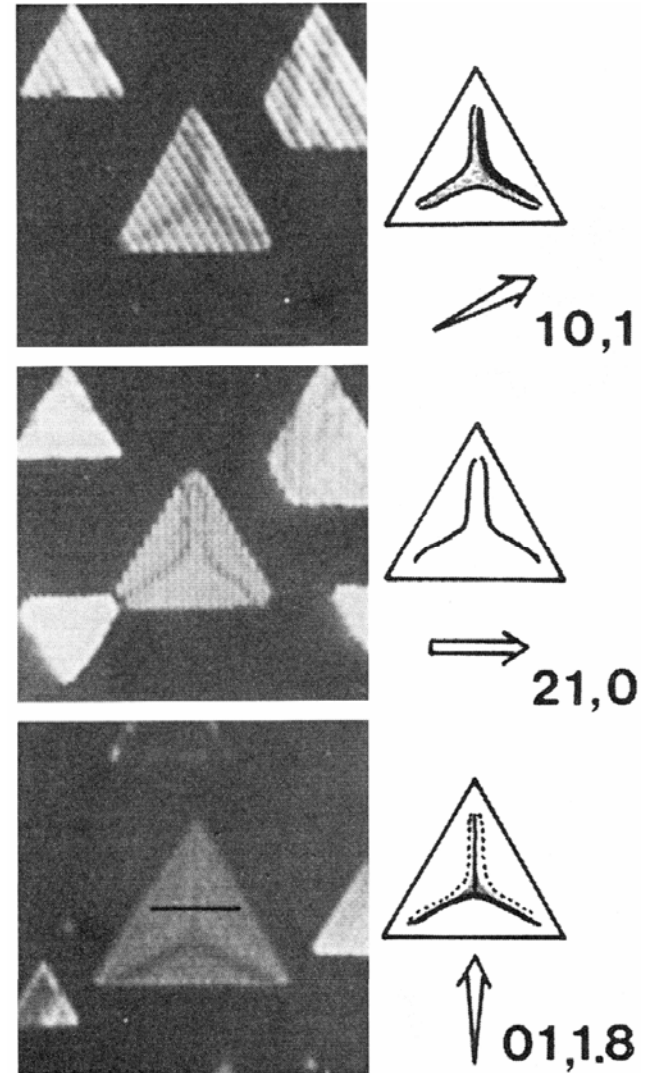


Surface effects & interfaces



Interface misfit dislocations are a common class of defects to image

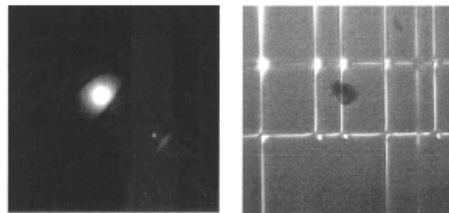
Be aware of surface relaxation effects (i.e. $\vec{g} \cdot \vec{b} \times \vec{u} \neq 0$)



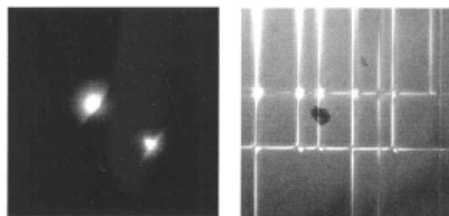
Surface effects & interfaces

400 two beam condition
Images are axial dark field

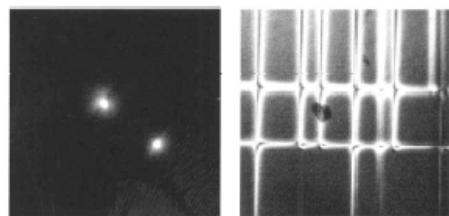
$s \gg 0$



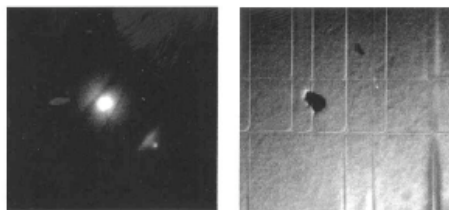
$s > 0$



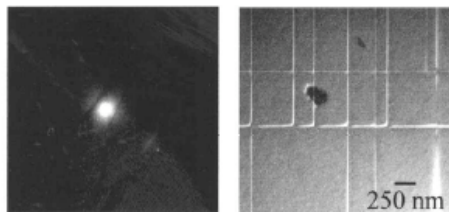
$s = 0$



$s < 0$

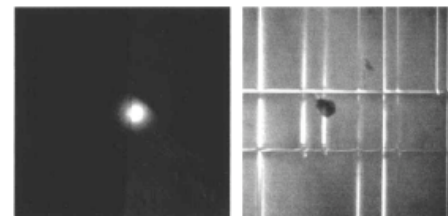


$s \ll 0$

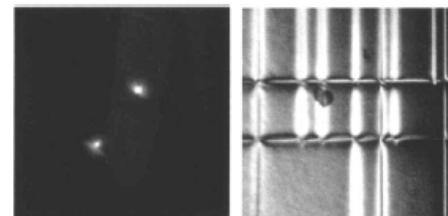


040 two beam condition
Images are axial dark field

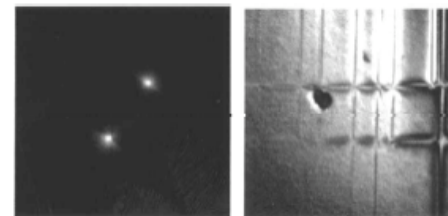
$s \gg 0$



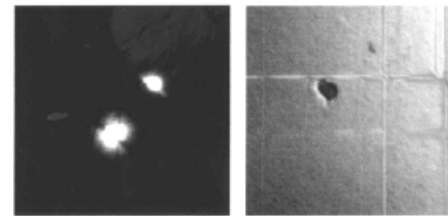
$s > 0$



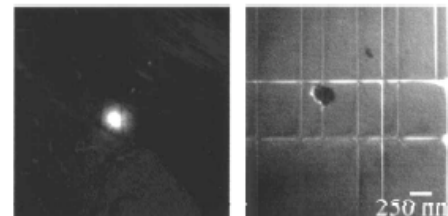
$s = 0$



$s < 0$



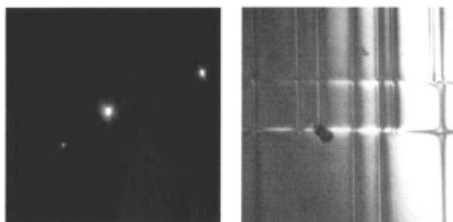
$s \ll 0$



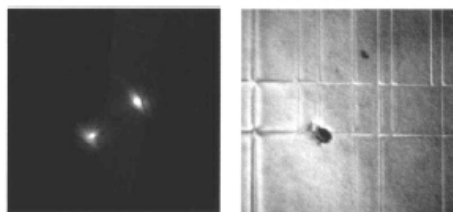
Surface effects & interfaces

311 two beam condition
Images are axial dark field

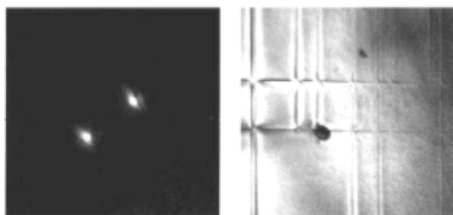
$s \gg 0$



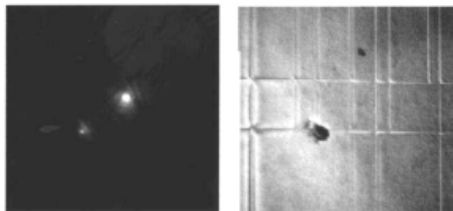
$s > 0$



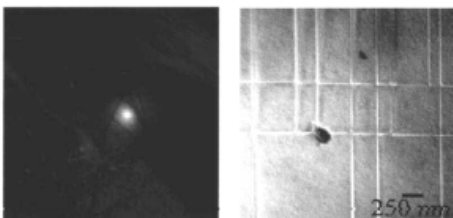
$s = 0$



$s < 0$

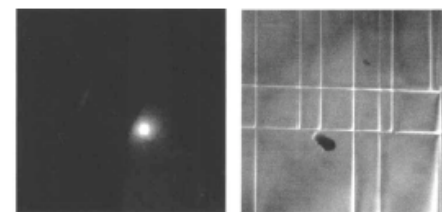


$s \ll 0$

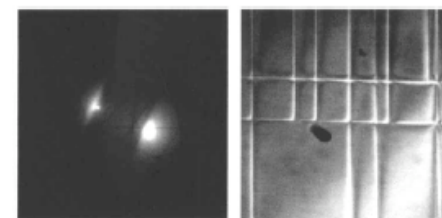


$13\bar{1}$ two beam condition
Images are axial dark field

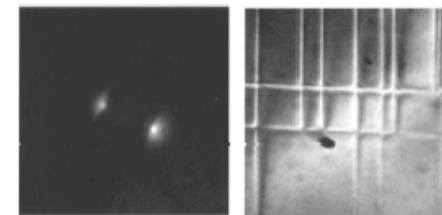
$s \gg 0$



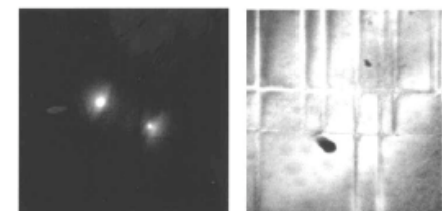
$s > 0$



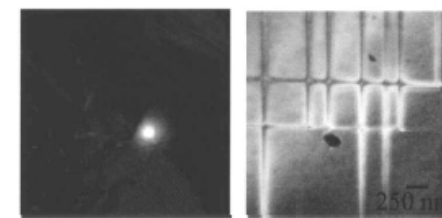
$s = 0$



$s < 0$



$s \ll 0$



Dislocation contrast

Consider a pure screw dislocation:

$$\vec{b}_e = 0 ; \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$$

$$\vec{R} = \dot{\mathbf{b}} \frac{\phi}{2\pi} = \frac{\dot{\mathbf{b}}}{2\pi} \tan\left(\frac{z - z_d}{x}\right)$$

So: $\vec{R} \propto \dot{\mathbf{b}}$

Thus: $\vec{g} \cdot \vec{R} \propto \vec{g} \cdot \dot{\mathbf{b}}$

“g dot b” contrast

Table 25.1. Different Burgers Vectors and Different Reflections Give Different $\mathbf{g} \cdot \mathbf{b} = n$ Values^a

$\mathbf{g} \backslash \mathbf{b}$	$\frac{1}{6} [11\bar{2}]$	$\frac{1}{6} [1\bar{2}1]$	$\frac{1}{6} [\bar{2}11]$	$\frac{1}{3} [111]$
$\pm(1\bar{1}1)$	$\pm 1/3$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$
$\pm(\bar{1}\bar{1}1)$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$	$\pm 1/3$
$\pm(0\bar{2}2)$	± 1	± 1	0	0
$\pm(200)$	$\pm 1/3$	$\pm 1/3$	$\pm 2/3$	$\pm 2/3$
$\pm(3\bar{1}1)$	0	± 1	± 1	± 1
$\pm(\bar{3}\bar{1}1)$	± 1	0	± 1	± 1

^aThe dislocations all lie on a (111) plane in an fcc material; the beam direction is [011].

Dislocation contrast

More to it (unfortunately)

Firstly, what is 'invisible'?

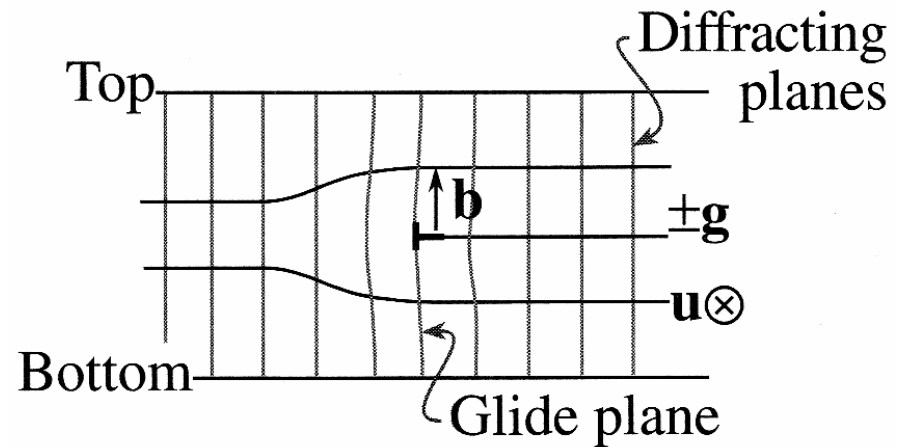
Generally if $\vec{g} \cdot \vec{b} < \frac{1}{3}$ the contrast is faint

More importantly, even if

$\vec{g} \cdot \vec{b} = 0$ can have $\vec{g} \cdot \vec{b} \times \vec{u} \neq 0$

So, really need to find conditions where both $\vec{g} \cdot \vec{b} = 0$ & $\vec{g} \cdot \vec{b} \times \vec{u} = 0$ if possible

May have to settle for $\vec{g} \cdot \vec{b} = 0$ & $\vec{g} \cdot \vec{b} \times \vec{u} \leq 0.64$



Dislocation contrast

Consider a pure screw dislocation:

$$\vec{b}_e = 0 ; \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$$

$$\vec{R} = \dot{\mathbf{b}} \frac{\phi}{2\pi} = \frac{\dot{\mathbf{b}}}{2\pi} \tan\left(\frac{z - z_d}{x}\right)$$

So: $\vec{R} \propto \dot{\mathbf{b}}$

Thus: $\vec{g} \cdot \vec{R} \propto \vec{g} \cdot \dot{\mathbf{b}}$

“g dot b” contrast

Table 25.1. Different Burgers Vectors and Different Reflections Give Different $\mathbf{g} \cdot \mathbf{b} = n$ Values^a

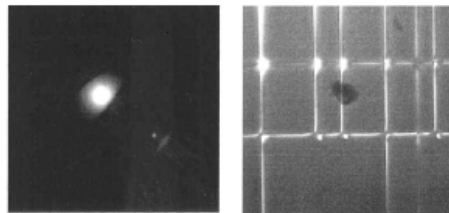
$\mathbf{g} \backslash \mathbf{b}$	$\frac{1}{6} [11\bar{2}]$	$\frac{1}{6} [1\bar{2}1]$	$\frac{1}{6} [\bar{2}11]$	$\frac{1}{3} [111]$
$\pm(1\bar{1}1)$	$\pm 1/3$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$
$\pm(\bar{1}\bar{1}1)$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$	$\pm 1/3$
$\pm(0\bar{2}2)$	± 1	± 1	0	0
$\pm(200)$	$\pm 1/3$	$\pm 1/3$	$\pm 2/3$	$\pm 2/3$
$\pm(3\bar{1}1)$	0	± 1	± 1	± 1
$\pm(\bar{3}\bar{1}1)$	± 1	0	± 1	± 1

^aThe dislocations all lie on a (111) plane in an fcc material; the beam direction is [011].

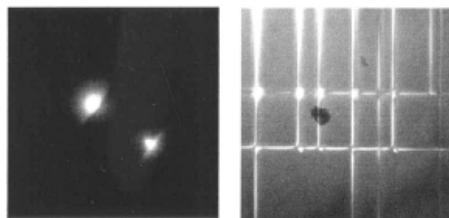
Surface effects & interfaces

400 two beam condition
Images are axial dark field

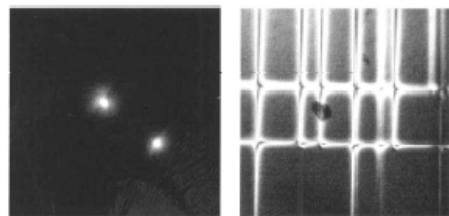
$s \gg 0$



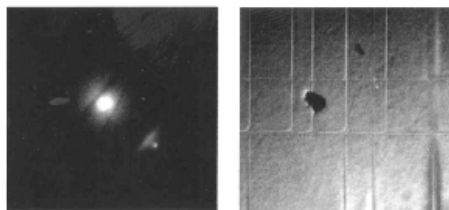
$s > 0$



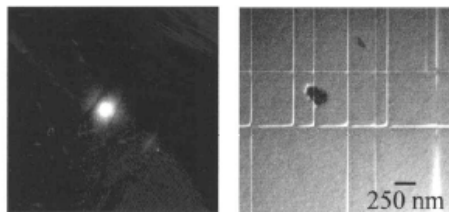
$s = 0$



$s < 0$

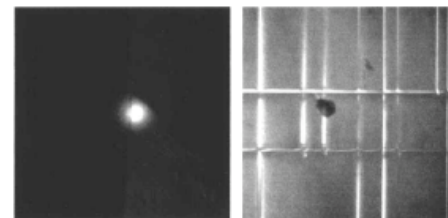


$s \ll 0$

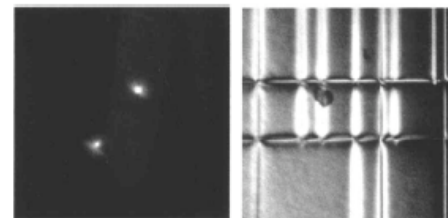


040 two beam condition
Images are axial dark field

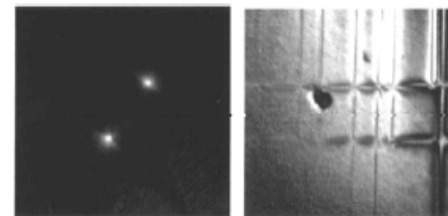
$s \gg 0$



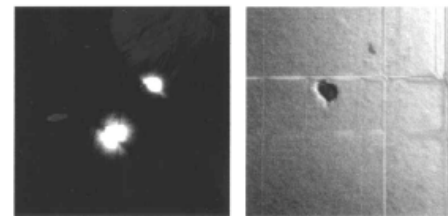
$s > 0$



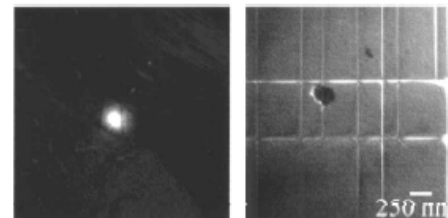
$s = 0$



$s < 0$



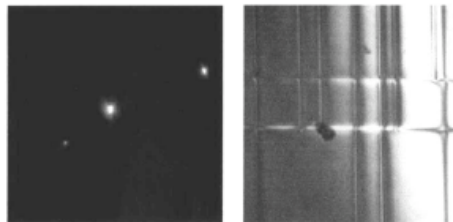
$s \ll 0$



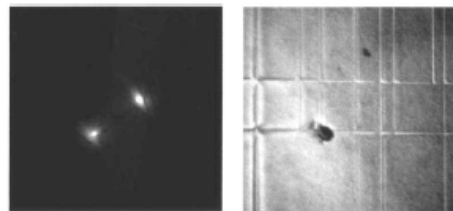
Surface effects & interfaces

311 two beam condition
Images are axial dark field

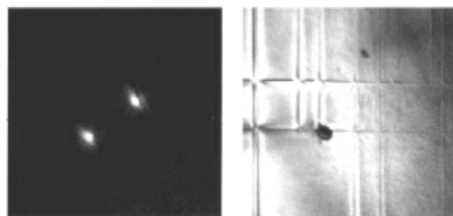
$s \gg 0$



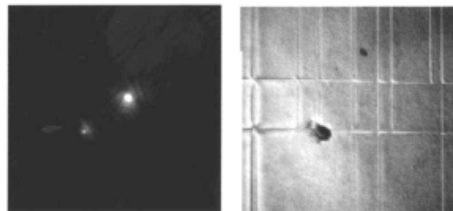
$s > 0$



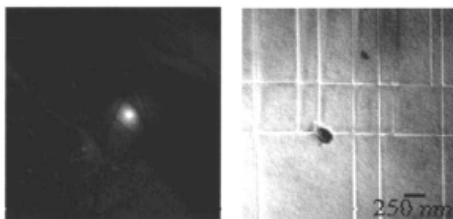
$s = 0$



$s < 0$

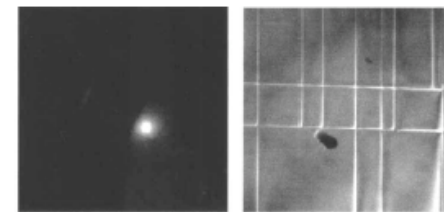


$s \ll 0$

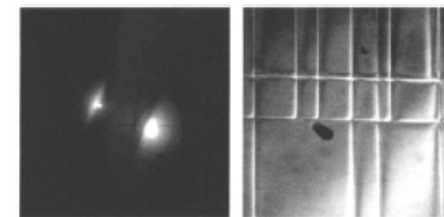


$13\bar{1}$ two beam condition
Images are axial dark field

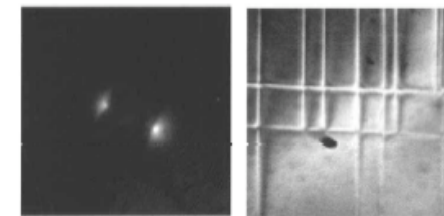
$s \gg 0$



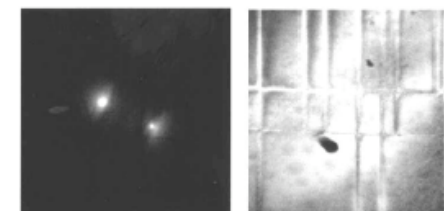
$s > 0$



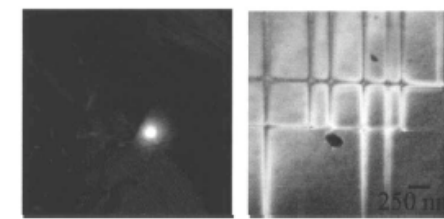
$s = 0$



$s < 0$



$s \ll 0$



Surface effects & interfaces

An example: Interfacial misfit dislocations in SiGe

For details, see Stach, et al, *Phil Mag* **80**, 2000.

Table A 1. Diffraction conditions for which $\mathbf{g} \cdot \mathbf{b} = 0$ is true for at least one Burgers vector.

\mathbf{g}	$\mathbf{b} = \frac{a}{2}[0\bar{1}1]$	$\mathbf{b} = \frac{a}{2}[\bar{1}01]$	$\mathbf{b} = \frac{a}{2}[011]$	$\mathbf{b} = \frac{a}{2}[101]$
400	0	2	0	2
040	2	0	2	0
311	0	1	1	2
$13\bar{1}$	2	1	1	0

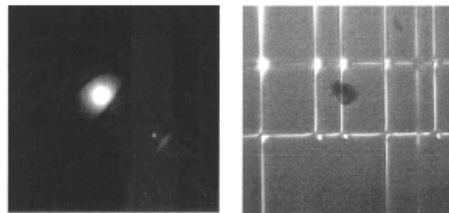
Table A 2. List of $|\mathbf{g} \cdot \mathbf{b}|$, $|\mathbf{g} \cdot \mathbf{b} \times \mathbf{u}|$ and m for each of the slip systems for the four diffraction conditions shown in Table A 1.

\mathbf{g}	$ \mathbf{g} \cdot \mathbf{b} $	$ \mathbf{g} \cdot \mathbf{b} \times \mathbf{u} $	$m = \frac{1}{2} \mathbf{g} \cdot \mathbf{b} \times \mathbf{u} $
		$\mathbf{b}, (a/2)[0\bar{1}1]; \mathbf{u}, [\bar{1}10]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	0	$5/2\sqrt{2}$	0.22
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[\bar{1}01]; \mathbf{u}, [\bar{1}10]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	1	$5/2\sqrt{2}$	0.22
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[011]; \mathbf{u}, [\bar{1}10]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$5/2\sqrt{2}$	0.22
		$\mathbf{b}, (a/2)[101]; \mathbf{u}, [\bar{1}10]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	2	$3/2\sqrt{2}$	0.13
$13\bar{1}$	0	$5/2\sqrt{2}$	0.22
		$\mathbf{b}, (a/2)[0\bar{1}1]; \mathbf{u}, [110]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	0	$1/2\sqrt{2}$	0.05 ←
$13\bar{1}$	1	$1/2\sqrt{2}$	0.05 ←
		$\mathbf{b}, (a/2)[\bar{1}01]; \mathbf{u}, [110]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[011]; \mathbf{u}, [110]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[101]; \mathbf{u}, [110]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	2	$1/2\sqrt{2}$	0.05 ←
$13\bar{1}$	0	$1/2\sqrt{2}$	0.05 ←

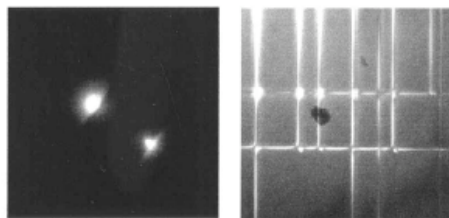
Surface effects & interfaces

400 two beam condition
Images are axial dark field

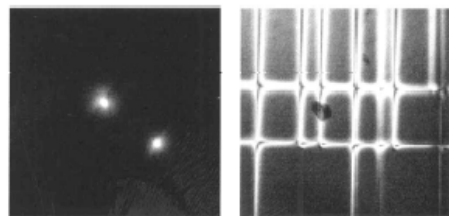
$s \gg 0$



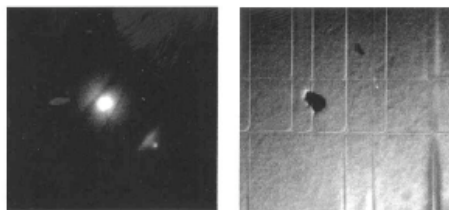
$s > 0$



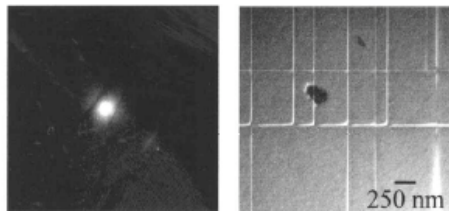
$s = 0$



$s < 0$

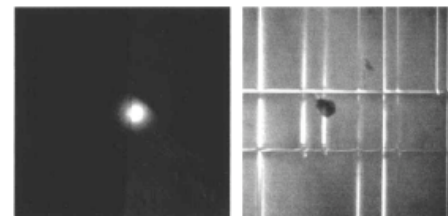


$s \ll 0$

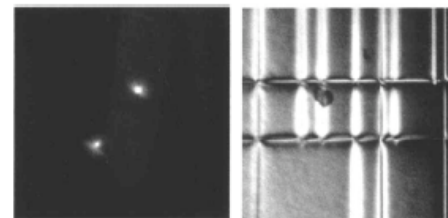


040 two beam condition
Images are axial dark field

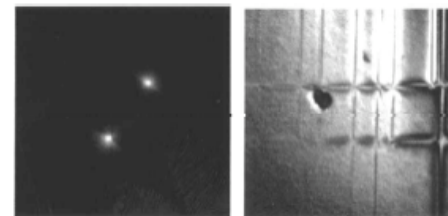
$s \gg 0$



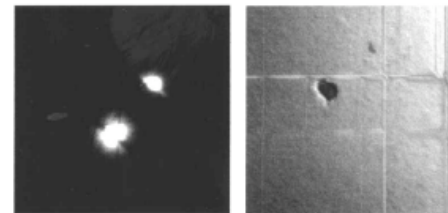
$s > 0$



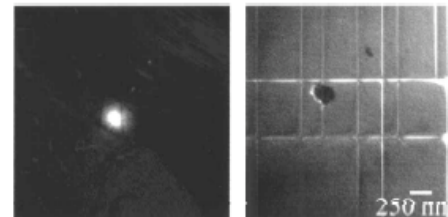
$s = 0$



$s < 0$



$s \ll 0$



Surface effects & interfaces

An example: Interfacial misfit dislocations in SiGe

For details, see Stach, et al, *Phil Mag* **80**, 2000.

Table A 1. Diffraction conditions for which $\mathbf{g} \cdot \mathbf{b} = 0$ is true for at least one Burgers vector.

\mathbf{g}	$\mathbf{b} = \frac{a}{2}[0\bar{1}1]$	$\mathbf{b} = \frac{a}{2}[\bar{1}01]$	$\mathbf{b} = \frac{a}{2}[011]$	$\mathbf{b} = \frac{a}{2}[101]$
400	0	2	0	2
040	2	0	2	0
311	0	1	1	2
$13\bar{1}$	2	1	1	0

Table A 2. List of $|\mathbf{g} \cdot \mathbf{b}|$, $|\mathbf{g} \cdot \mathbf{b} \times \mathbf{u}|$ and m for each of the slip systems for the four diffraction conditions shown in Table A 1.

\mathbf{g}	$ \mathbf{g} \cdot \mathbf{b} $	$ \mathbf{g} \cdot \mathbf{b} \times \mathbf{u} $	$m = \frac{1}{2} \mathbf{g} \cdot \mathbf{b} \times \mathbf{u} $
		$\mathbf{b}, (a/2)[0\bar{1}1]; \mathbf{u}, [\bar{1}10]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	0	$5/2\sqrt{2}$	0.22
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[\bar{1}01]; \mathbf{u}, [\bar{1}10]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	1	$5/2\sqrt{2}$	0.22
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[011]; \mathbf{u}, [\bar{1}10]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$5/2\sqrt{2}$	0.22
		$\mathbf{b}, (a/2)[101]; \mathbf{u}, [\bar{1}10]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	2	$3/2\sqrt{2}$	0.13
$13\bar{1}$	0	$5/2\sqrt{2}$	0.22
		$\mathbf{b}, (a/2)[0\bar{1}1]; \mathbf{u}, [110]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	0	$1/2\sqrt{2}$	0.05 ←
$13\bar{1}$	1	$1/2\sqrt{2}$	0.05 ←
		$\mathbf{b}, (a/2)[\bar{1}01]; \mathbf{u}, [110]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[011]; \mathbf{u}, [110]$	
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
		$\mathbf{b}, (a/2)[101]; \mathbf{u}, [110]$	
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	2	$1/2\sqrt{2}$	0.05 ←
$13\bar{1}$	0	$1/2\sqrt{2}$	0.05 ←

Dislocation contrast

Consider a pure screw dislocation:

$$\vec{b}_e = 0 ; \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$$

$$\vec{R} = \dot{\mathbf{b}} \frac{\phi}{2\pi} = \frac{\dot{\mathbf{b}}}{2\pi} \tan\left(\frac{z - z_d}{x}\right)$$

So: $\vec{R} \propto \dot{\mathbf{b}}$

Thus: $\vec{g} \cdot \vec{R} \propto \vec{g} \cdot \dot{\mathbf{b}}$

“g dot b” contrast

Table 25.1. Different Burgers Vectors and Different Reflections Give Different $\mathbf{g} \cdot \mathbf{b} = n$ Values^a

$\mathbf{g} \backslash \mathbf{b}$	$\frac{1}{6} [11\bar{2}]$	$\frac{1}{6} [1\bar{2}1]$	$\frac{1}{6} [\bar{2}11]$	$\frac{1}{3} [111]$
$\pm(1\bar{1}1)$	$\pm 1/3$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$
$\pm(\bar{1}\bar{1}1)$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$	$\pm 1/3$
$\pm(0\bar{2}2)$	± 1	± 1	0	0
$\pm(200)$	$\pm 1/3$	$\pm 1/3$	$\pm 2/3$	$\pm 2/3$
$\pm(3\bar{1}1)$	0	± 1	± 1	± 1
$\pm(\bar{3}\bar{1}1)$	± 1	0	± 1	± 1

^aThe dislocations all lie on a (111) plane in an fcc material; the beam direction is [011].

Surface effects & interfaces

An example: Interfacial misfit dislocations in SiGe

For details, see Stach, et al, *Phil Mag* **80**, 2000.

Table A 1. Diffraction conditions for which $\mathbf{g} \cdot \mathbf{b} = 0$ is true for at least one Burgers vector.

\mathbf{g}	$\mathbf{b} = \frac{a}{2}[0\bar{1}1]$	$\mathbf{b} = \frac{a}{2}[\bar{1}01]$	$\mathbf{b} = \frac{a}{2}[011]$	$\mathbf{b} = \frac{a}{2}[101]$
400	0	2	0	2
040	2	0	2	0
311	0	1	1	2
$13\bar{1}$	2	1	1	0

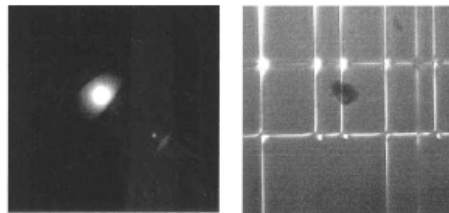
Table A 2. List of $|\mathbf{g} \cdot \mathbf{b}|$, $|\mathbf{g} \cdot \mathbf{b} \times \mathbf{u}|$ and m for each of the slip systems for the four diffraction conditions shown in Table A 1.

\mathbf{g}	$ \mathbf{g} \cdot \mathbf{b} $	$ \mathbf{g} \cdot \mathbf{b} \times \mathbf{u} $	$m = \frac{1}{2} \mathbf{g} \cdot \mathbf{b} \times \mathbf{u} $
$\mathbf{b}, (a/2)[0\bar{1}1]; \mathbf{u}, [\bar{1}10]$			
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	0	$5/2\sqrt{2}$	0.22
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
$\mathbf{b}, (a/2)[\bar{1}01]; \mathbf{u}, [\bar{1}10]$			
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	1	$5/2\sqrt{2}$	0.22
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
$\mathbf{b}, (a/2)[011]; \mathbf{u}, [\bar{1}10]$			
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$5/2\sqrt{2}$	0.22
$\mathbf{b}, (a/2)[101]; \mathbf{u}, [\bar{1}10]$			
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	2	$3/2\sqrt{2}$	0.13
$13\bar{1}$	0	$5/2\sqrt{2}$	0.22
$\mathbf{b}, (a/2)[0\bar{1}1]; \mathbf{u}, [110]$			
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	0	$1/2\sqrt{2}$	0.05 ←
$13\bar{1}$	1	$1/2\sqrt{2}$	0.05 ←
$\mathbf{b}, (a/2)[\bar{1}01]; \mathbf{u}, [110]$			
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
$\mathbf{b}, (a/2)[011]; \mathbf{u}, [110]$			
400	0	$\sqrt{2}$	0.18
040	2	$\sqrt{2}$	0.18
311	1	$3/2\sqrt{2}$	0.13
$13\bar{1}$	1	$3/2\sqrt{2}$	0.13
$\mathbf{b}, (a/2)[101]; \mathbf{u}, [110]$			
400	2	$\sqrt{2}$	0.18
040	0	$\sqrt{2}$	0.18
311	2	$1/2\sqrt{2}$	0.05 ←
$13\bar{1}$	0	$1/2\sqrt{2}$	0.05 ←

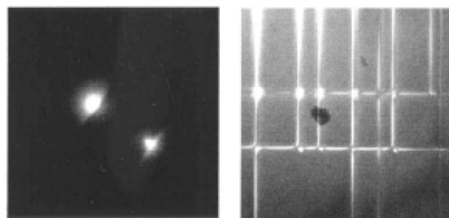
Surface effects & interfaces

400 two beam condition
Images are axial dark field

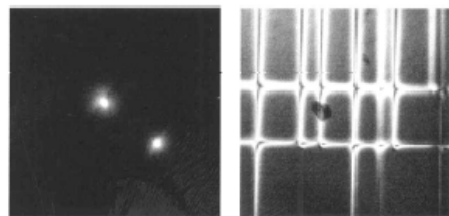
$s \gg 0$



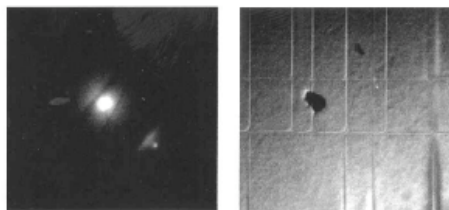
$s > 0$



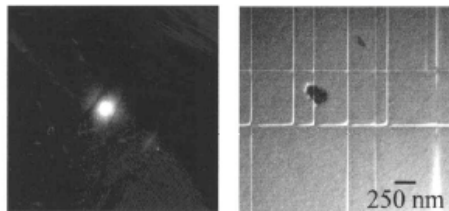
$s = 0$



$s < 0$

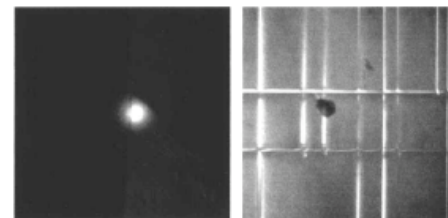


$s \ll 0$

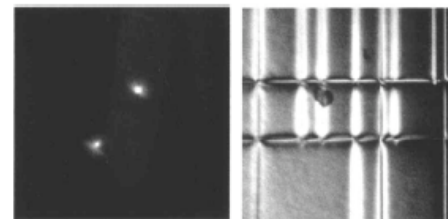


040 two beam condition
Images are axial dark field

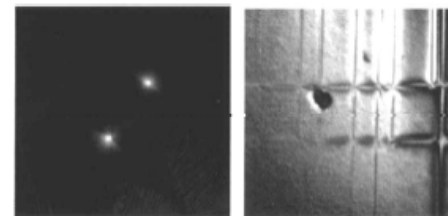
$s \gg 0$



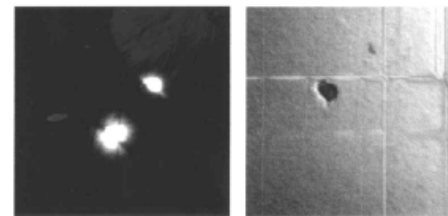
$s > 0$



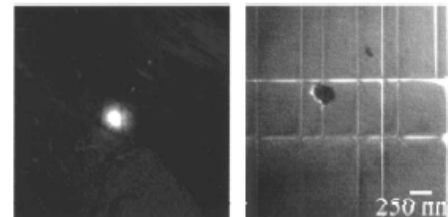
$s = 0$



$s < 0$



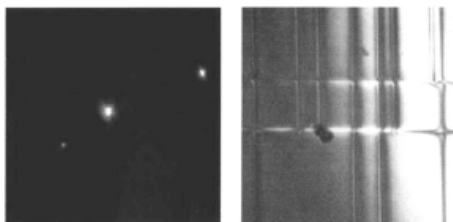
$s \ll 0$



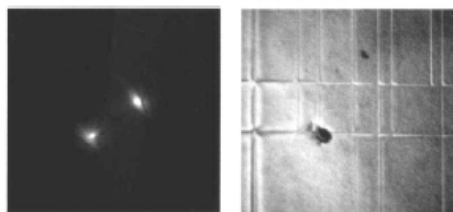
Surface effects & interfaces

311 two beam condition
Images are axial dark field

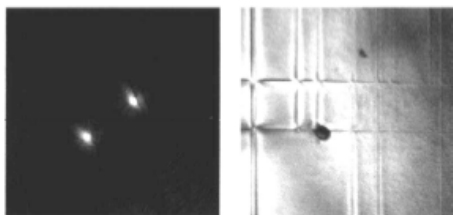
$s \gg 0$



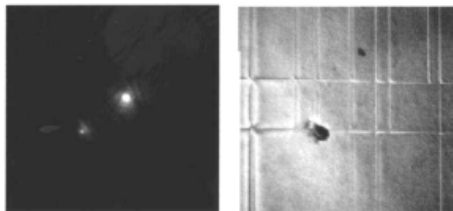
$s > 0$



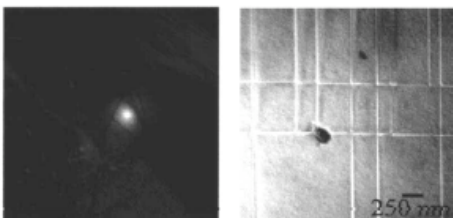
$s = 0$



$s < 0$

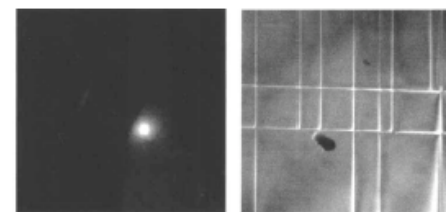


$s \ll 0$

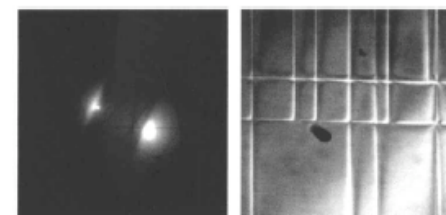


$1\bar{3}\bar{1}$ two beam condition
Images are axial dark field

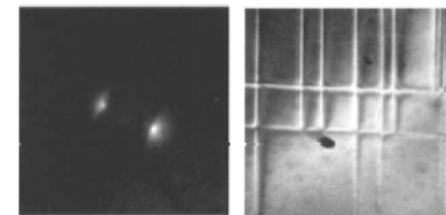
$s \gg 0$



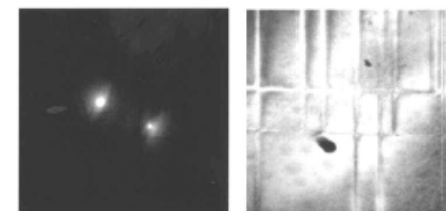
$s > 0$



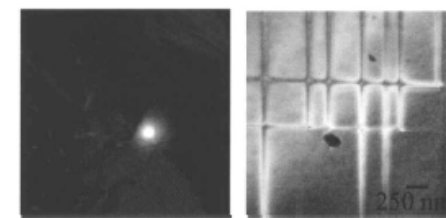
$s = 0$



$s < 0$



$s \ll 0$



Dislocation contrast

Consider a pure screw dislocation:

$$\vec{b}_e = 0 ; \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$$

$$\vec{R} = \dot{\mathbf{b}} \frac{\phi}{2\pi} = \frac{\dot{\mathbf{b}}}{2\pi} \tan\left(\frac{z - z_d}{x}\right)$$

So: $\vec{R} \propto \dot{\mathbf{b}}$

Thus: $\vec{g} \cdot \vec{R} \propto \vec{g} \cdot \dot{\mathbf{b}}$

“g dot b” contrast

Table 25.1. Different Burgers Vectors and Different Reflections Give Different $\mathbf{g} \cdot \mathbf{b} = n$ Values^a

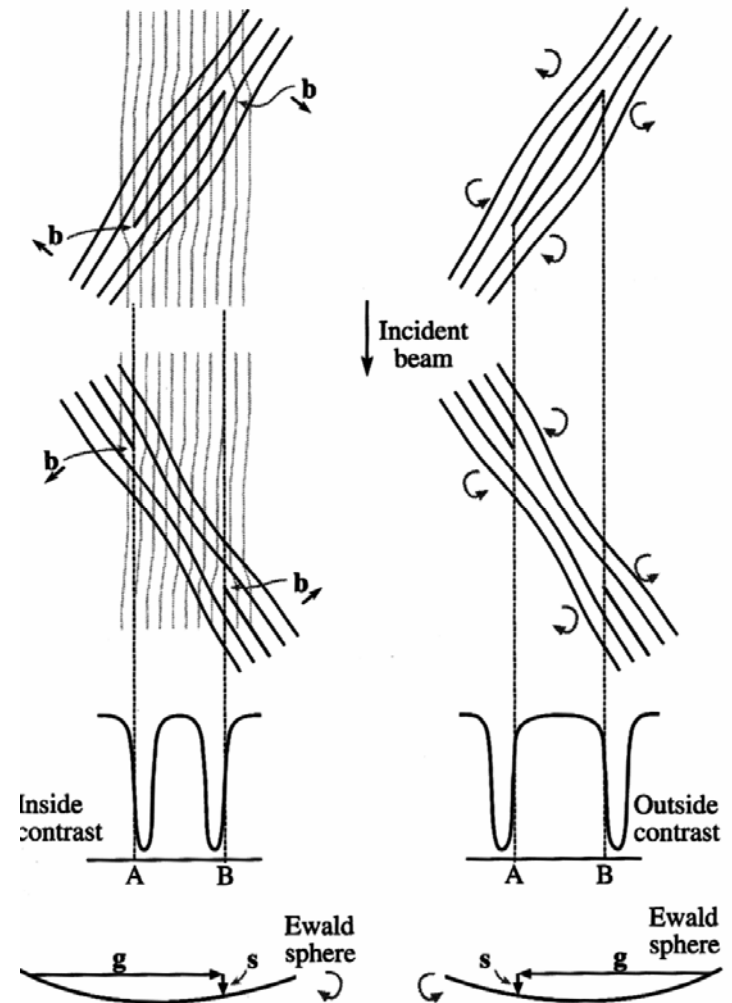
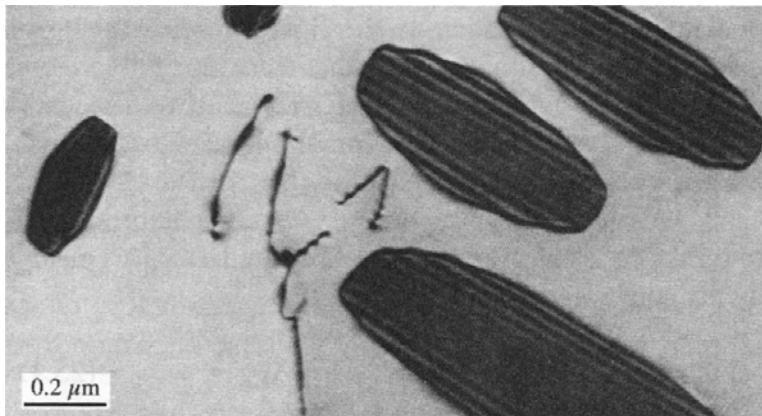
$\mathbf{g} \backslash \mathbf{b}$	$\frac{1}{6} [11\bar{2}]$	$\frac{1}{6} [1\bar{2}1]$	$\frac{1}{6} [\bar{2}11]$	$\frac{1}{3} [111]$
$\pm(1\bar{1}1)$	$\pm 1/3$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$
$\pm(\bar{1}\bar{1}1)$	$\pm 2/3$	$\pm 1/3$	$\pm 1/3$	$\pm 1/3$
$\pm(0\bar{2}2)$	± 1	± 1	0	0
$\pm(200)$	$\pm 1/3$	$\pm 1/3$	$\pm 2/3$	$\pm 2/3$
$\pm(3\bar{1}1)$	0	± 1	± 1	± 1
$\pm(\bar{3}\bar{1}1)$	± 1	0	± 1	± 1

^aThe dislocations all lie on a (111) plane in an fcc material; the beam direction is [011].

Dislocation loops & dipoles

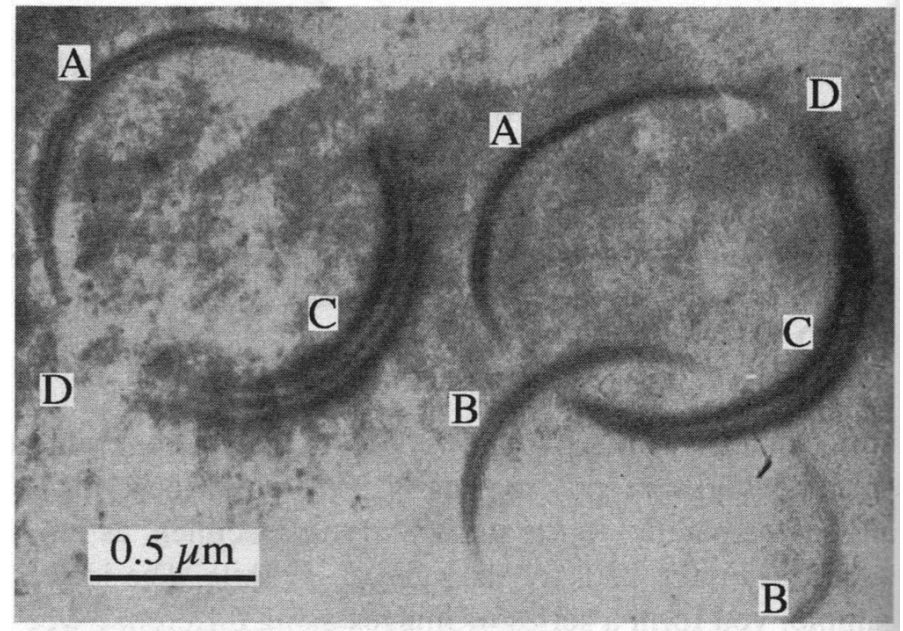
Often dislocation loops formed by collapse of interstitials or vacancies

Can thus enclose intrinsic or extrinsic stacking faults, or may be no fault



Dislocations loops & dipoles

Prismatic dislocation loops
can nicely demonstrate
 $\vec{g} \cdot \dot{\mathbf{b}} = 0$ & $\vec{g} \cdot \dot{\mathbf{b}} \times \dot{\mathbf{u}} = 0$
effects



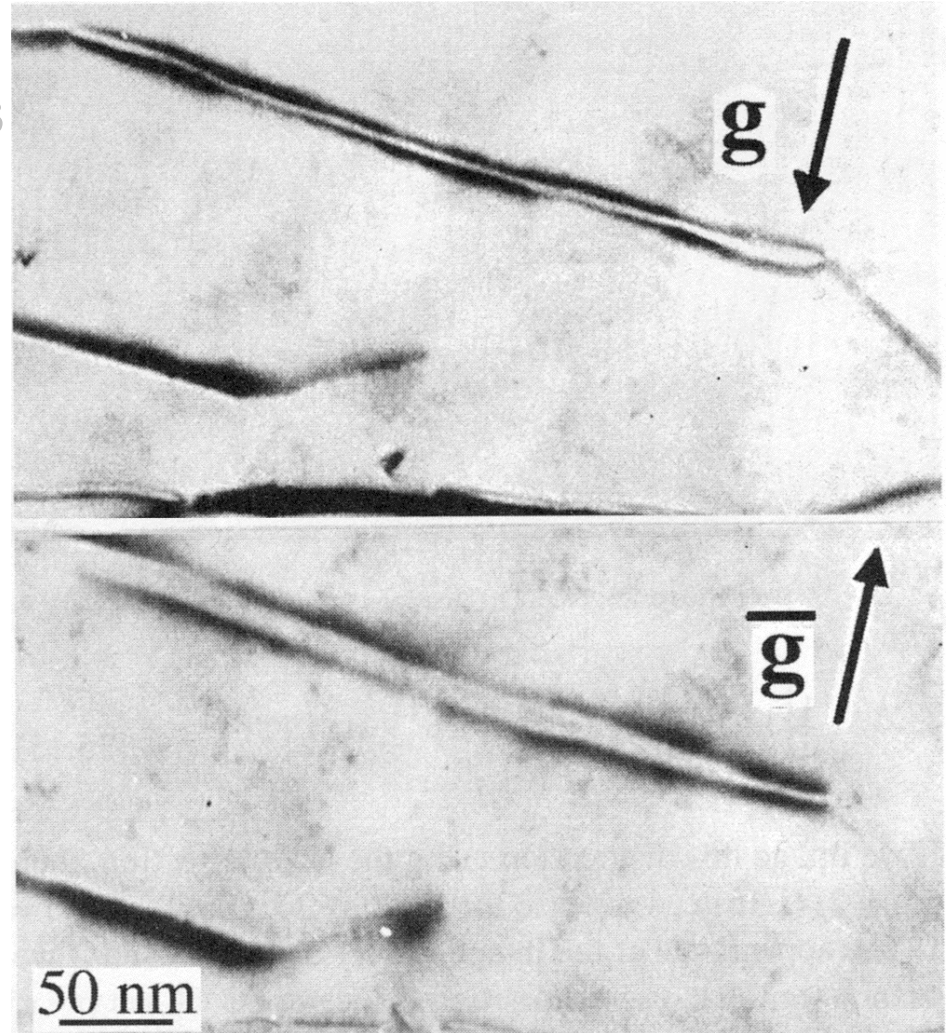
Dislocations loops & dipoles

Dislocation dipoles are essentially elongated loops

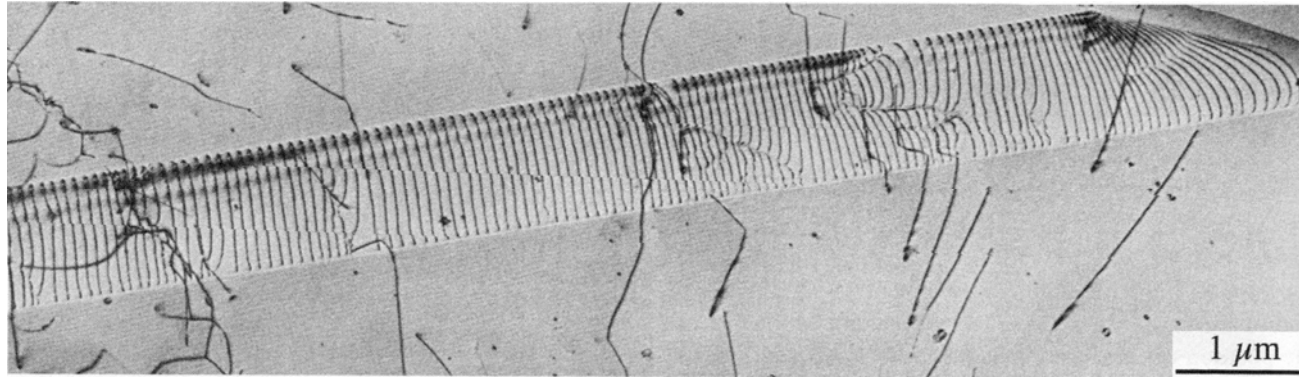
Have no net Burgers vector, and thus no long range stress field

Exhibit same 'inside / outside' contrast on reverse of s

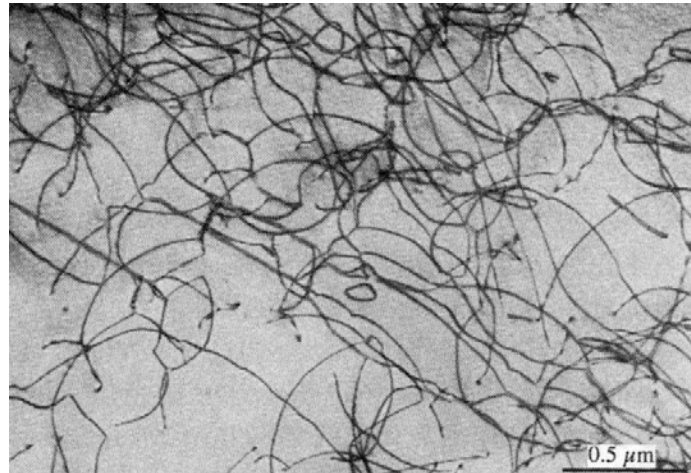
- Remember contrast origin tied to $(\vec{g} \cdot \vec{b})_s$



Dislocations interactions & tangles



HVEM Image of slip along an inclined plane



A complex dislocation tangle

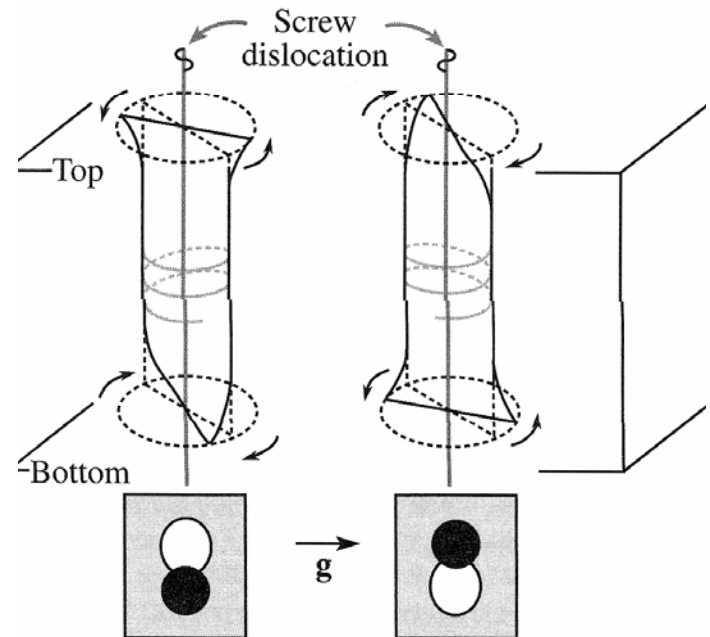
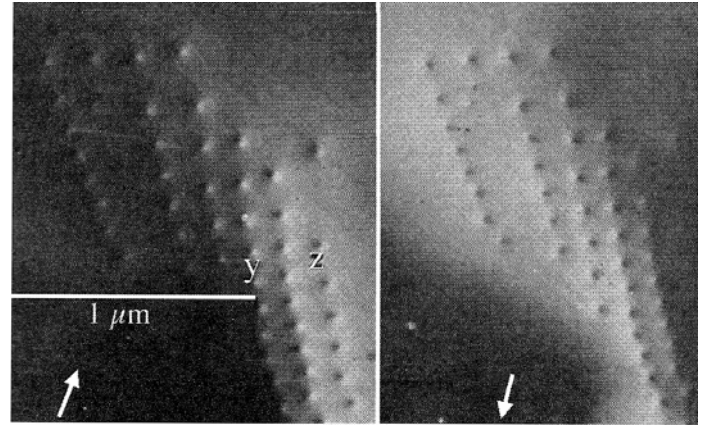
Cold rolled alloy



Surface effects & interfaces

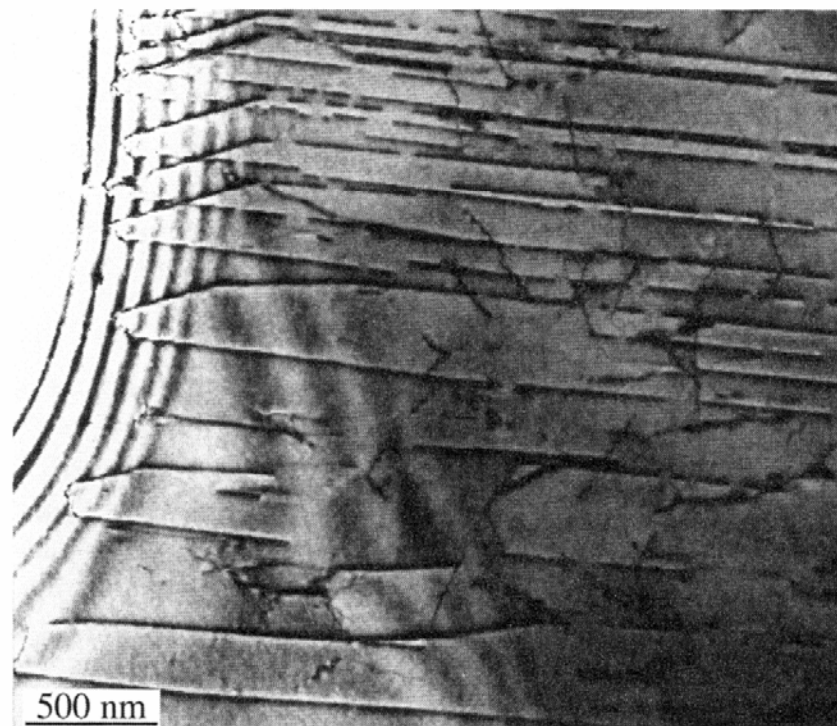
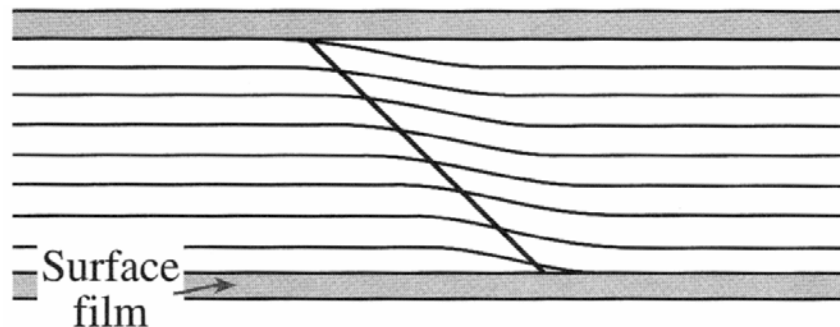
For a screw dislocation,
only worry about $\vec{g} \cdot \dot{\mathbf{b}} = 0$

However, even if $\vec{g} \cdot \dot{\mathbf{b}} = 0$
can see effects of surface
relaxation

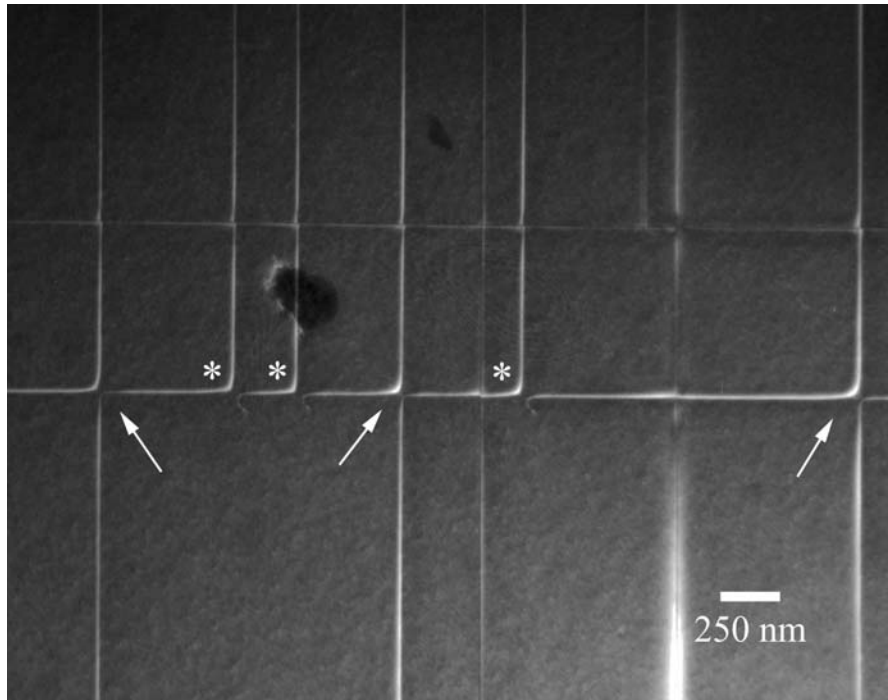


Surface effects & interfaces

Oxides on TEM samples
(an artifact) can pin
dislocations

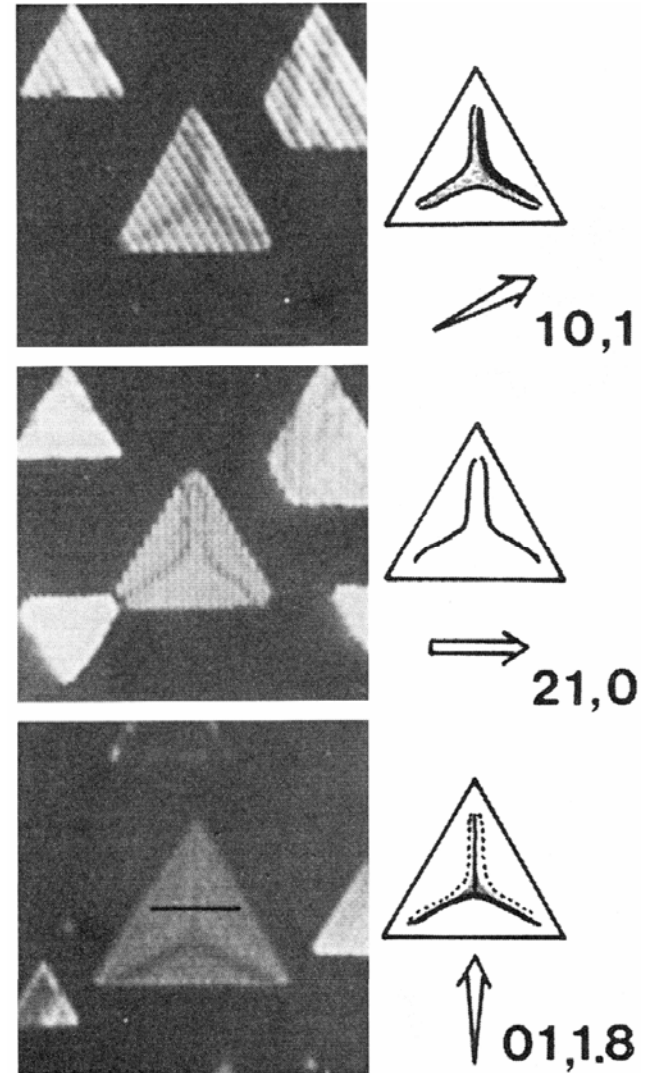


Surface effects & interfaces



Interface misfit dislocations are a common class of defects to image

Be aware of surface relaxation effects (i.e. $\vec{g} \cdot \vec{b} \times \vec{u} \neq 0$)



Coherent precipitates & islands

Strain field from coherent precipitates also give “g dot b contrast”

A line of zero contrast is observed perpendicular to g

