

# CHM 696-11: Week 8

Instructor: Alexander Wei

## Optical Properties of Metal Nanoparticles and Nanoparticle Assemblies

Review:

Wei, Q.; Wei, A. In *Supramolecular Chemistry of Organic–Inorganic Hybrid Materials* (Chapter 10), Mañez, R. M.; Rurack, K., Eds.; Wiley and Sons: New York, 2010; pp. 319-349

# Plasmon-resonant nanoparticles

**Surface plasmon (SP):** collective excitation of conduction electrons, using light at a resonant (visible to NIR) frequency

## Plasmon-enhanced extinction:

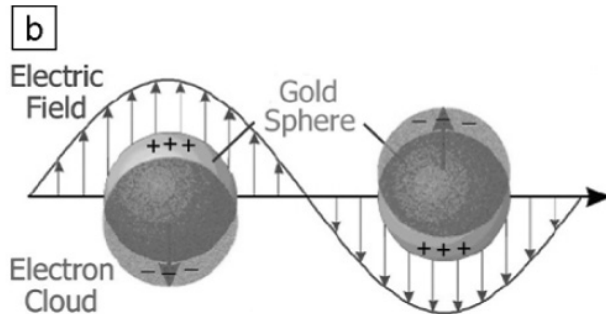
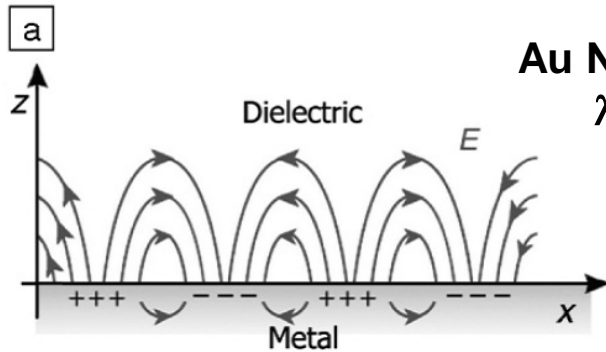
$$\epsilon = 10^9 - 10^{11} \text{ M}^{-1} \text{ cm}^{-1}$$

$$C_{\text{sca}} = 10^{-13} - 10^{-9} \text{ cm}^2$$

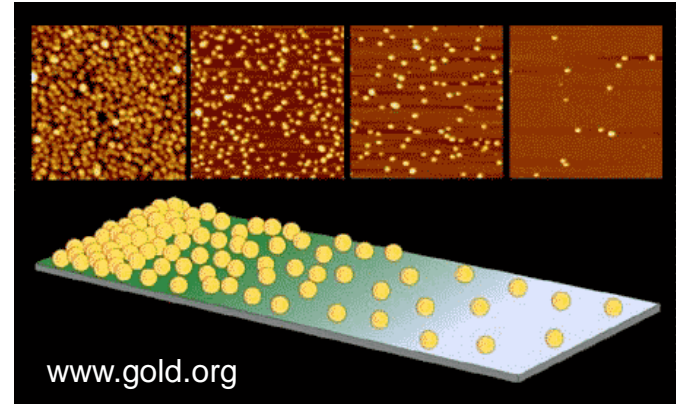
$$\phi_{\text{sca}} = 0.04 - 0.90$$

Ag NPs (20–150 nm):  
 $\lambda_{\text{SP}} = 380 - 600 \text{ nm}$

Au NPs (20–150 nm):  
 $\lambda_{\text{SP}} = 520 - 660 \text{ nm}$



## Scattering from single Au nanospheres



Absorption: **red**

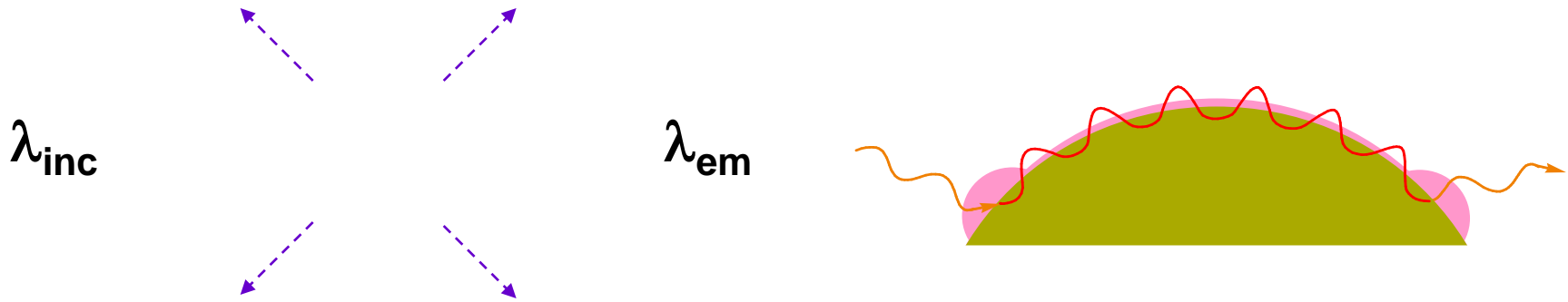
Scattering: **green**

**Lycurgus Cup,**  
 4th century A.D.

(Ag-Au NP's  
 embedded in  
 glass)

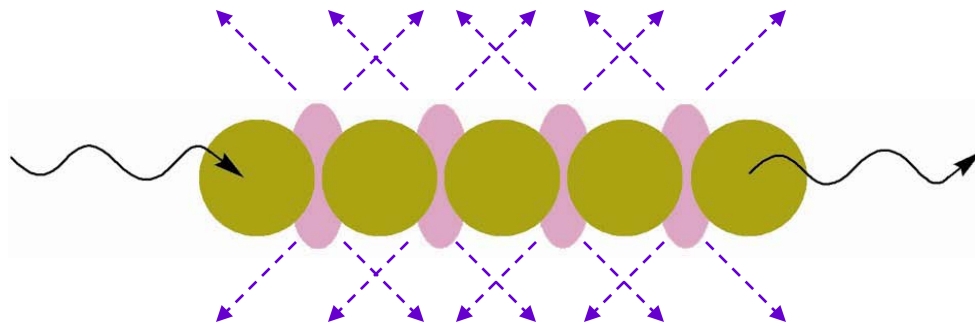


# Manifestations of Surface Plasmons



I. Localized surface plasmon resonance (LSPR) in metal nanoparticles ( $d < \lambda_p$ )

II. Surface plasmon waves (polaritons) propagating along smooth metal surface ( $d > \lambda_p$ )



III. Coupled plasmons in nanoparticle aggregate or array

For a primer on surface plasmons, see: *Nanoparticles: Building Blocks for Nanotechnology*, Ed. V. M. Rotello, Kluwer Academics: New York, 2004; Chapter 7 (Wei)

# Physical description of localized SPRs

## Free-electron behavior in metals: the Drude model

Polarizability or oscillator strength  $\alpha$  defined by the Clausius-Mosotti (a.k.a. Lorentz-Lorenz) equation:

$$\alpha = 4\pi\epsilon_0 R^3 \left| \frac{\epsilon - \epsilon_d}{\epsilon + 2\epsilon_d} \right|$$

Complex dielectric function  $\epsilon = \epsilon'(\omega) + i\epsilon''(\omega)$ ;

Resonance achieved with  $\epsilon'(\omega) = -2\epsilon_d$ ,  $\epsilon''(\omega) \ll 1$

Given a plasma frequency  $\omega_p$  such that  $\epsilon(\omega_p) = 0$ :

$$\epsilon'(\omega) \approx 1 - \frac{\omega_p^2}{\omega^2 + \Gamma^2} \quad \epsilon''(\omega) \approx \frac{\omega_p^2 \Gamma}{\omega(\omega^2 + \Gamma^2)}$$

where  $\Gamma$  is the plasma relaxation frequency.

$$\text{Ideally, } \omega_{SP} \approx \frac{\omega_p}{\sqrt{2\epsilon_d + 1}}$$

However, free-electron response is coupled with interband transitions (e.g., Au(5d $\rightarrow$ 6s)), which changes  $\omega_{SP}$

Only metals with low  $\epsilon''(\omega)$  at  $\omega_{SP}$  will exhibit strong plasmon resonance: **Ag > Au > Cu**

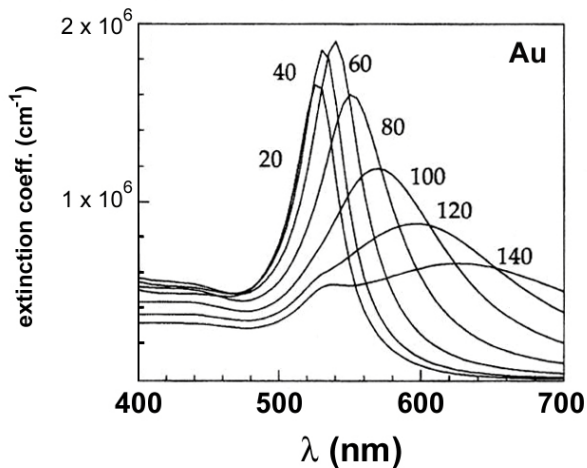
# Physical description of plasmons (cont'd)

## Electrodynamic Mie Theory

Can calculate dipolar optical response with great accuracy, especially if performed under “quasi-static” conditions (valid when particle size is less than 30 nm)

## Generalized Mie Theory:

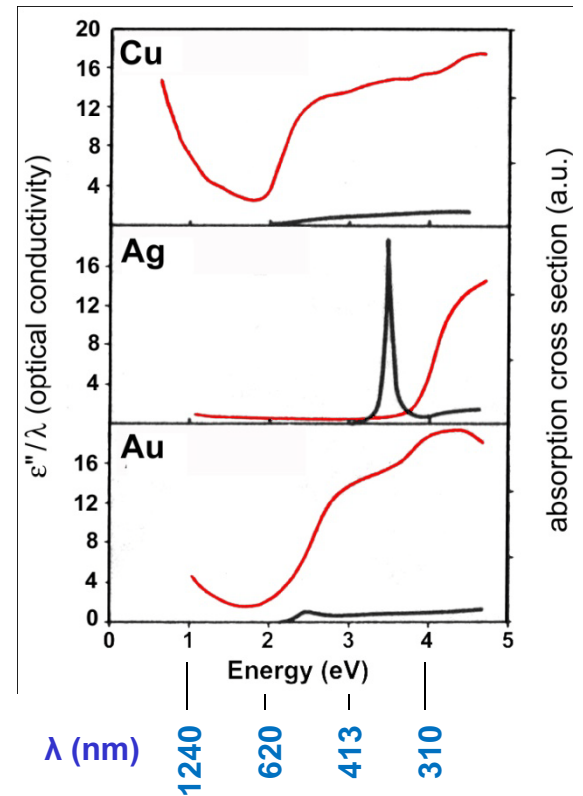
Can calculate approximate optical response for metal nanoparticles of all shapes and sizes; accounts for higher-order effects such as phase retardation, quadrupolar resonances, etc.



Calculated plasmon response from spherical Au nanoparticles in H<sub>2</sub>O:

Yguerabide, *Anal. Biochem.* **1998**, 262, 137.

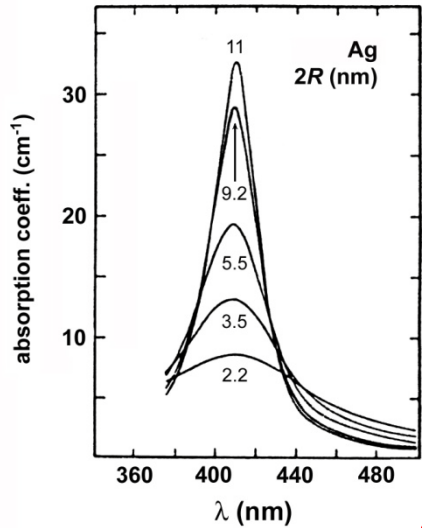
Calculated response (extinction) from metal nanoparticles (in air):



$$\text{eV-to-}\lambda \text{ (nm) conversion: } \lambda = \frac{1239}{\text{eV}}$$

Kriebig and Vollmer, *Optical Properties of Metal Clusters*, c.1995.

# Size effects on localized SPRs

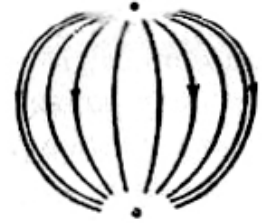


Surface scattering of oscillating electrons: plasmon lineshape ( $I$ ) broadens with  $1/R$

Phase retardation: redshift and broadening of  $\lambda_{SP}$  for particles greater than  $L_E$ , the electron mean free path (40-50 nm)

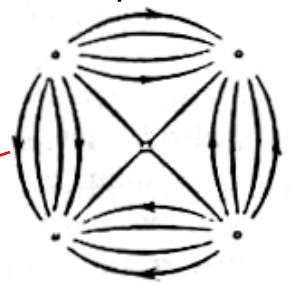
Higher-order plasmon resonances: increase in probability with larger particle size (also a function of  $L_E$ )

Dipolar mode



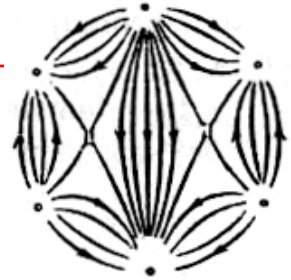
Electric field L = 1

Quadrupolar mode

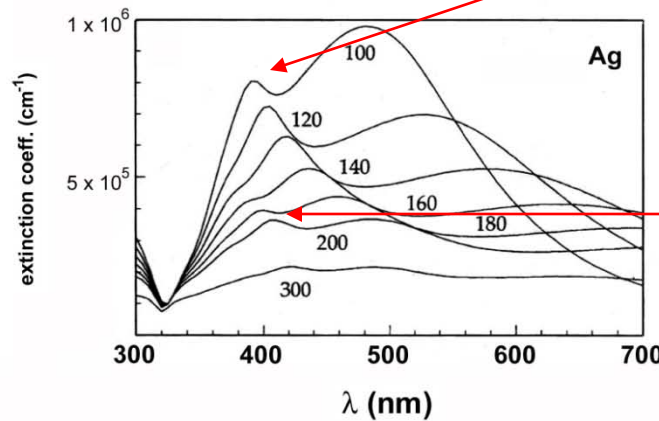
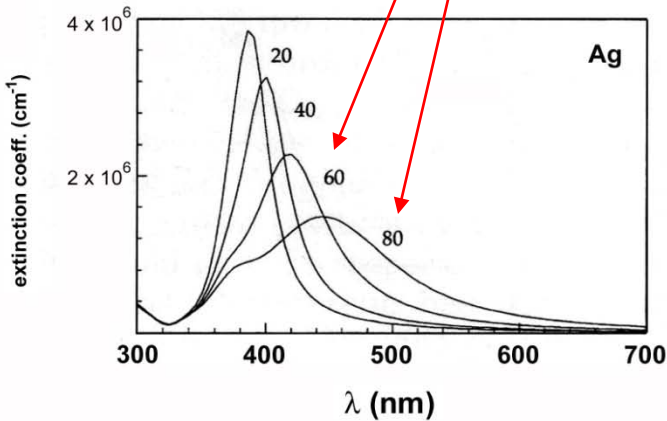


Electric field L = 2

Octupolar mode



Electric field L = 3



Calculated plasmon response from spherical Ag nanoparticles in H<sub>2</sub>O:  
Yguerabide, *Anal. Biochem.* **1998**, 262, 137.